

Ice flow sensitivity to boundary processes: A coupled model study in the Vostok Subglacial Lake area

Malte Thoma,^{1,2} Klaus Grosfeld,² Christoph Mayer,¹ Frank Pattyn³

¹*Bavarian Academy of Sciences, Commission for Glaciology, Alfons-Goppel-Str. 11 80539 Munich, Germany*

²*Alfred Wegener Institute for Polar and Marine Research, Bussestrasse 24, 27570 Bremerhaven, Germany*

³*Laboratoire de Glaciologie, Département des Sciences de la Terre et de l'Environnement (DSTE), Université Libre de Bruxelles (ULB), CP 160/03, Avenue F.D. Roosevelt, B-1050 Bruxelles, Belgium*

ABSTRACT. Several hundred subglacial lakes have been identified beneath Antarctica so far. Their interaction with the overlying ice sheet and their influence on ice dynamics are still subject of investigation. While it is known that lakes reduce the ice sheet friction towards a free slip basal boundary condition, little is known about how basal melting and freezing at the lake-ice interface modifies the ice dynamics, thermal regime, and ice rheology. In this diagnostic study we simulate the Vostok Subglacial Lake area with a coupled Full Stokes 3D-ice-flow model and a 3D-lake-circulation model. The exchange of energy (heat) and mass at the lake-ice interface increases (decreases) the temperature in the ice column above the lake by up to 10% in freezing (melting) areas, resulting in a significant modification of the highly nonlinear ice viscosity. We show that basal lubrication at the ice sheet's bottom has a significant impact not only on the ice flow above the lake itself, but also on the vicinity and far field. While the ice flow crosses Vostok Subglacial Lake flow divergence is observed and modelled. The heterogeneous basal-mass-balance pattern at the lake-ice interface intensifies this divergence. Instead of interactive coupling between the ice-flow model and the lake-flow model only a single iteration is required for a realistic representation of the ice-water interaction. Additionally, our study indicates that simplified parametrizations of the surface temperature boundary condition might lead to a velocity error of 20% for the area of investigation.

INTRODUCTION

Subglacial lakes are common and widespread beneath the Antarctic Ice Sheet. More than 370 of these lakes have been identified so far (Wright and Siegert, 2010), but just 72 exceed an area of 10 km². The largest one, Vostok Subglacial Lake¹, located in East Antarctica (Figure 1a) measures 16 000 km² (Studinger and others, 2004; Filina and others, 2008). Subglacial lakes are identified from satellite images by their surface, which is flat compared to the surrounding ice sheet. These lakes have been isolated from direct exchange with the atmosphere by several kilometers of ice for millions of years and hence provide a unique environment for potential life forms. Drilling at Vostok Station revealed that not only melting takes place at the ice's base, but that water also refreezes at the lake-ice interface (Jouzel and others, 1999; Siegert and others, 2001). At Vostok Station a 210 m-thick layer of accreted lake-ice was discovered between the meteoric ice and the lake's surface. Tikku and others (2004) were able to estimate the distribution of accreted ice by ice-penetrating radar feature tracking. However, until

drilling into subglacial lakes, as suggested by Woodward and others (2010), provides in-situ information, numerical models are needed to quantify processes at the lake-ice interface (Williams, 2001; Mayer and others, 2003; Thoma and others, 2007, 2008a, 2009, 2010b; Woodward and others, 2010). According to Bell and others (2007) the storage capacity of subglacial lakes should be considered in ice-sheet mass bal-

ance assessments. The role of these lakes for the subglacial hydrology is still not clear, but there are indications of an active hydrological system underneath the ice sheet, which affects the general ice dynamics (Wingham and others, 2006; Fricker and others, 2007; Bell and others, 2011) and might trigger the onset of fast-flowing ice streams by basal lubrication (Bell and others, 2007; Kohler, 2007; Stearns and others, 2008).

The ice flow depends on the temperature-dependent viscosity of the ice body. The viscosity is modified by basal melting and freezing, which induce vertical velocities at the ice base in the order of centimeters per year. A coupled modelling approach with an idealised setting has been applied recently in order to investigate the interaction of subglacial lakes with the overlying ice sheet (Thoma and others, 2010a).

In this study we take a further step and investigate the impact of different forcings such as surface temperature, basal mass exchange, and basal friction on the ice flow in the area of lake Vostok.

BOUNDARY CONDITIONS AND MODEL SETUP

In order to investigate the area around Vostok Subglacial Lake in a numerical model study, surface elevation and bedrock for the entire model domain were taken from the BEDMAP data set (Lythe and others, 2001). To acquire a more realistic representation of the lake Vostok domain, we merged the most up-to-date regional bedrock geometry model by Fil-

¹According to the *U.S. Board on Geographic Names, Antarctica ID: 18528*, the official name of the lake is *Vostok Subglacial Lake*.

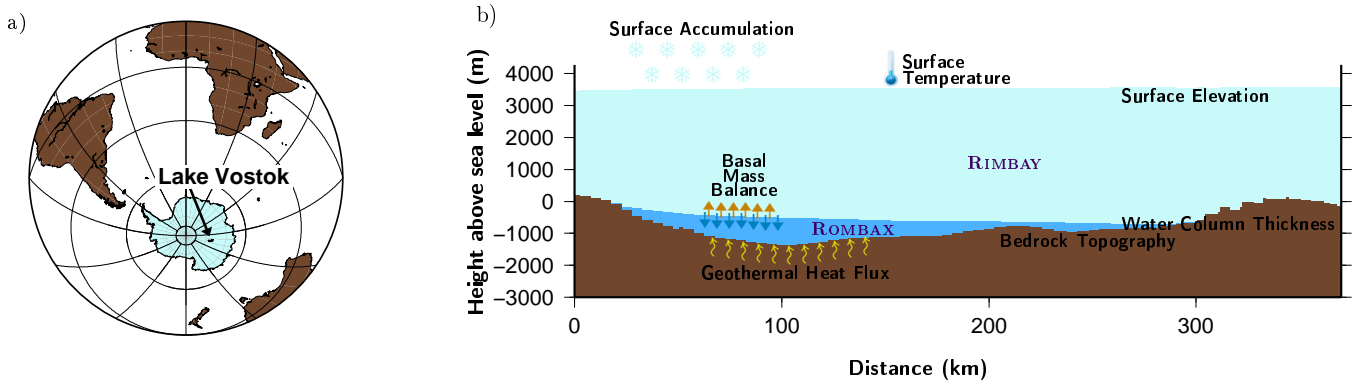


Fig. 1. a) Position of Vostok Subglacial Lake; the exact geographical location, with respect to longitude and latitude, is given in Figure 8a. b) Cross section through the lake along the profile shown in Figure 4a, indicating numerical model domains and boundary conditions.

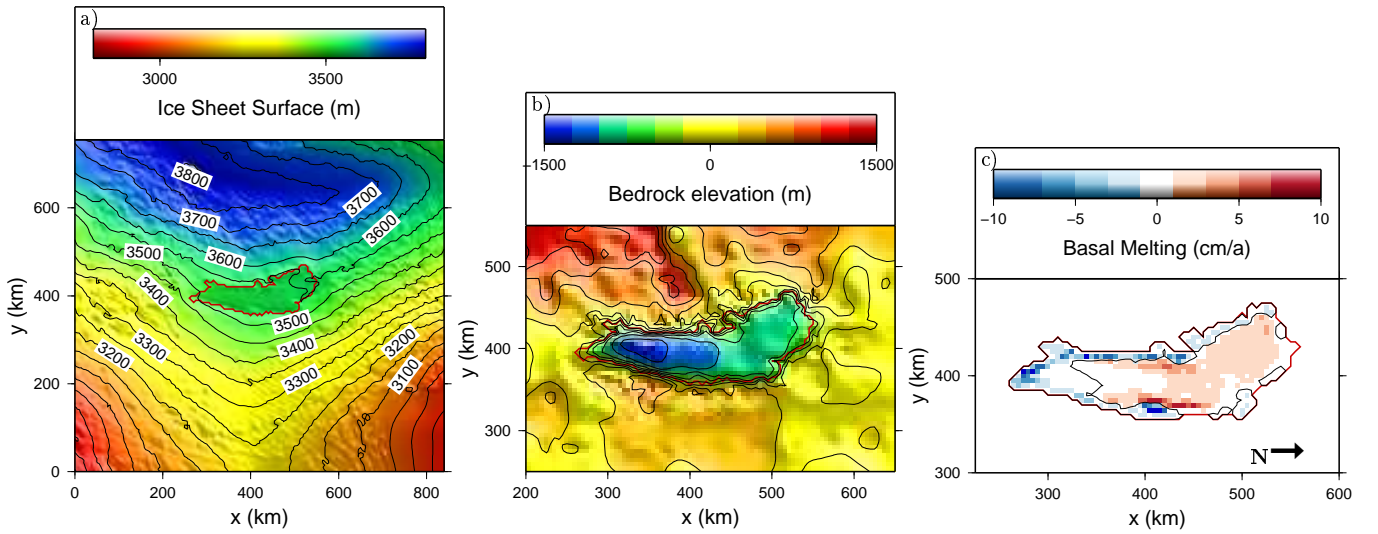


Fig. 2. a) Ice sheet surface and b) bedrock elevation in the Vostok Subglacial Lake area. Data according to Lythe and others (2001) improved according to Filina and others (2008). The solid red line indicates the lake's shoreline, determined by satellite imagery. c) Applied basal mass balance according to Thoma and others (2010b). Negative values represent basal freezing. The arrow indicates the geographic North. The full model domain is shown in a), b-c) indicate zoomed regions for an improved recognition of details.

Field	Source
General surface elevation and bedrock	BEDMAP (Lythe and others, 2001)
Improved surface elevation, bedrock, and water column thickness for the Vostok Subglacial Lake area	Filina and others (2008)
Surface accumulation	Arthern and others (2006)
Geothermal heat flux	Shapiro and Ritzwoller (2004)
Surface temperature	Huybrechts (1992), Comiso (2000), Wang and Hou (2009)
Basal mass balance	Interactively coupled according to Thoma and others (2010a,b)

Table 1. Summary of applied boundary conditions.

ina and others (2008) into the continental BEDMAP model (Figure 1b and 2a-b).

The *surface accumulation rate* is given by Arthern and others (2006). The initial temperature distribution within the ice is calculated according to Robin (1955), based on a spatially varying *surface temperature* and the basal pressure-dependent freezing point of the ice sheet base. Three different surface-temperature fields are applied (Figure 3): a simple latitude-height-parametrization after Huybrechts (1992), a data set based on satellite infrared measurements (Comiso, 2000; Le Brocq and others, 2010), and a data set derived from borehole measurements (Wang and Hou, 2009). The basal

geothermal heat flux is prescribed according to Shapiro and Ritzwoller (2004).

Ice flow across subglacial lakes and bedrock differs significantly in *basal friction* and *basal mass balance*. Basal friction is parametrised by a scalar friction coefficient β^2 (MacAyeal, 1993; Pattyn, 2003, 2008), which relates basal velocity (\vec{v}_b) to basal drag: $\vec{\tau}_b = \beta^2 \vec{v}_b$. Above subglacial lakes, a free slip condition ($\beta^2 = 0$) allows sliding. Above bedrock, $\beta^2 = 25\,000\text{ Pa a/m}$ corresponds to a typical basal frictional stress of about 100 kPa (Paterson, 1994) if a velocity of about 4 m/a is assumed. The basal mass balance (Figure 2c) is given by the lake-flow model ROMBAX (Thoma and others, 2010b). This

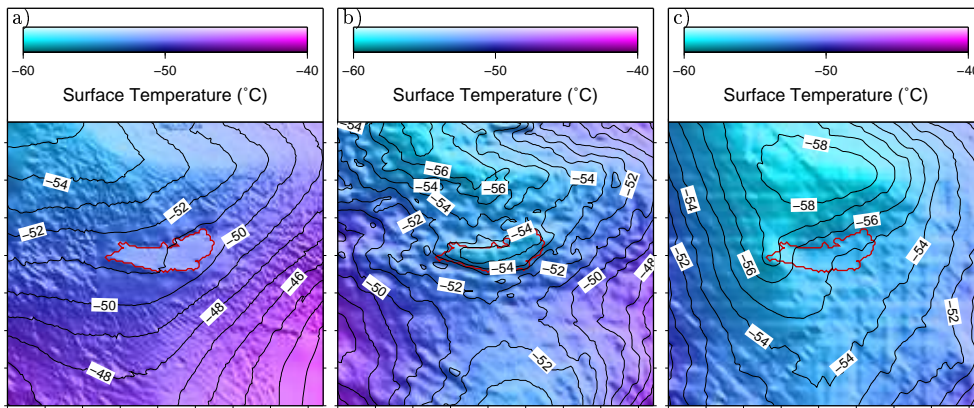


Fig. 3. Applied surface temperatures according to a) Huybrechts (1992), b) Comiso (2000), and c) Wang and Hou (2009).

general circulation model calculates the water circulation and the melting and freezing rates at the lake-ice boundary considering the pressure-dependent freezing point and the conservation of heat according to Holland and Jenkins (1999). All boundary conditions applied to force the ice flow model RIMBAY (Thoma and others, 2010a) are summarised in Table 1 and indicated in Figure 1.

The whole model domain is shown in Figure 2a. The ice divide, from where the ice approaches Vostok Subglacial Lake is included in the model domain, which renders specific lateral boundary conditions unnecessary. The horizontal resolution of the ice model RIMBAY is 5 km; in the vertical 40 terrain following layers are applied. The time step is dynamically adjusted according to the Courant-Friedrichs-Lewy (CFL) condition. The initial flow field starts from rest, and the model runs for 200 000 years in a shallow-ice-approximation (SIA) mode, until a preliminary steady state of the velocity- and temperature field is reached. After additional 50 000 model years, and the application of Full-Stokes Physics (e.g., Patyn, 2008), the model achieves a steady state. For this study the ice model runs in a diagnostic mode, keeping ice thickness, bedrock, lake volume, and grounding line position constant.

RESULTS

General flow and temperature regime above Vostok Subglacial Lake

Our modelled surface flow field across Vostok Subglacial Lake (Figure 4a) is in agreement with the modelling results of Patyn and others (2004). It shows a consistent pattern with flow directions similar to those indicated by radar-image feature tracking of Tikku and others (2004) and a *Vostok flow line* modelled by Salamatin and others (2009). Our modelled ice flow velocity at Vostok Station of about 4.0 m/a fits within the ice flow velocities observed (1.9–4.2 m/a) by Kwok and others (2000), Bell and others (2002), Tikku and others (2004), and Wendt and others (2005). Therefore, we consider the model realistic enough to investigate the impact of different boundary forcings with respect to the flow field.

Upstream of the lake, the modelled velocity ranges from about 3.0 m/a to 3.5 m/a. Across the lake, the frictionless bottom results in a general velocity acceleration. In the lake's center only a slight increase to about 3.6 m/a is modelled, but in the northern and southern part of the lake the velocity increase of up to 4.6 m/a and 4.1 m/a, respectively, is significant. The ice flow over Vostok Subglacial Lake diverges.

In particular, at the southern tip of the lake the flow is significantly diverted southward. These deflections correspond to the increased velocities at both ends of the lake. However, the reasons for these velocity increases are different: In the south, where freezing is strongest (comp. Figure 2c), ascending isotherms result in warmer ice (Figure 5) and hence in a reduced viscosity. Therefore, velocities are increased at the southern end of the lake. Beyond the lake, without basal freezing, the basal temperature cools down again, and hence the velocities decrease to their former magnitude. In contrast, the increased ice-surface gradient north-east of the lake (Figure 2a) results in a significant flow acceleration downstream of the lake of up to 6.5 m/a. This flow is channelled by a subglacial trough in this area (Figure 2b). The absence of basal friction over the lake results in *ice shelf* like flow in this area whereby ice over the northern part of the lake is dragged by the fast flowing ice beyond the lake. These findings are consistent with Bell and others (2007), who concluded that subglacial lakes initiate and maintain rapid ice flow through either active modification of the basal thermal regime of the ice sheet by lake accretion or through scouring bedrock channels in periodic drainage events.

Additional validation of the model results can be achieved by comparing the vertical temperature profile in the southern part of the lake with measurements from the Vostok-Station bore hole (e.g., Salamatin and others, 1994; Lipenkov and others, 2004). According to our modelling, only the surface temperature forcing of Wang and Hou (2009) is able to reproduce the observed temperatures in the upper part of the ice sheet. The two other available surface temperature data sets (Huybrechts, 1992; Comiso, 2000) result in too warm ice in the upper ice column. At the base the pressure-dependent melting point defines the basal temperature. Although measurements do not reach down to the lake-ice interface, the model results agree well with the available profile. In about 2000 m depth the modelled temperature (forced with the surface-temperature data of Wang and Hou, 2009) is up to 2°C above the in-situ temperature. This deviation may result from uncertainties of the modelled flow field, the assumed upstream surface temperatures and/or accumulation rate, or variations in the history of these parameters. Based on an assumed average ice flow velocity of 2 m/a and a distance of 200 km from the ice divide (comp. Figures 2a and 4a), variations of the surface boundary conditions during the last 100 000 years would be necessary to model a more realistic temperature profile. However, for the scope of this study

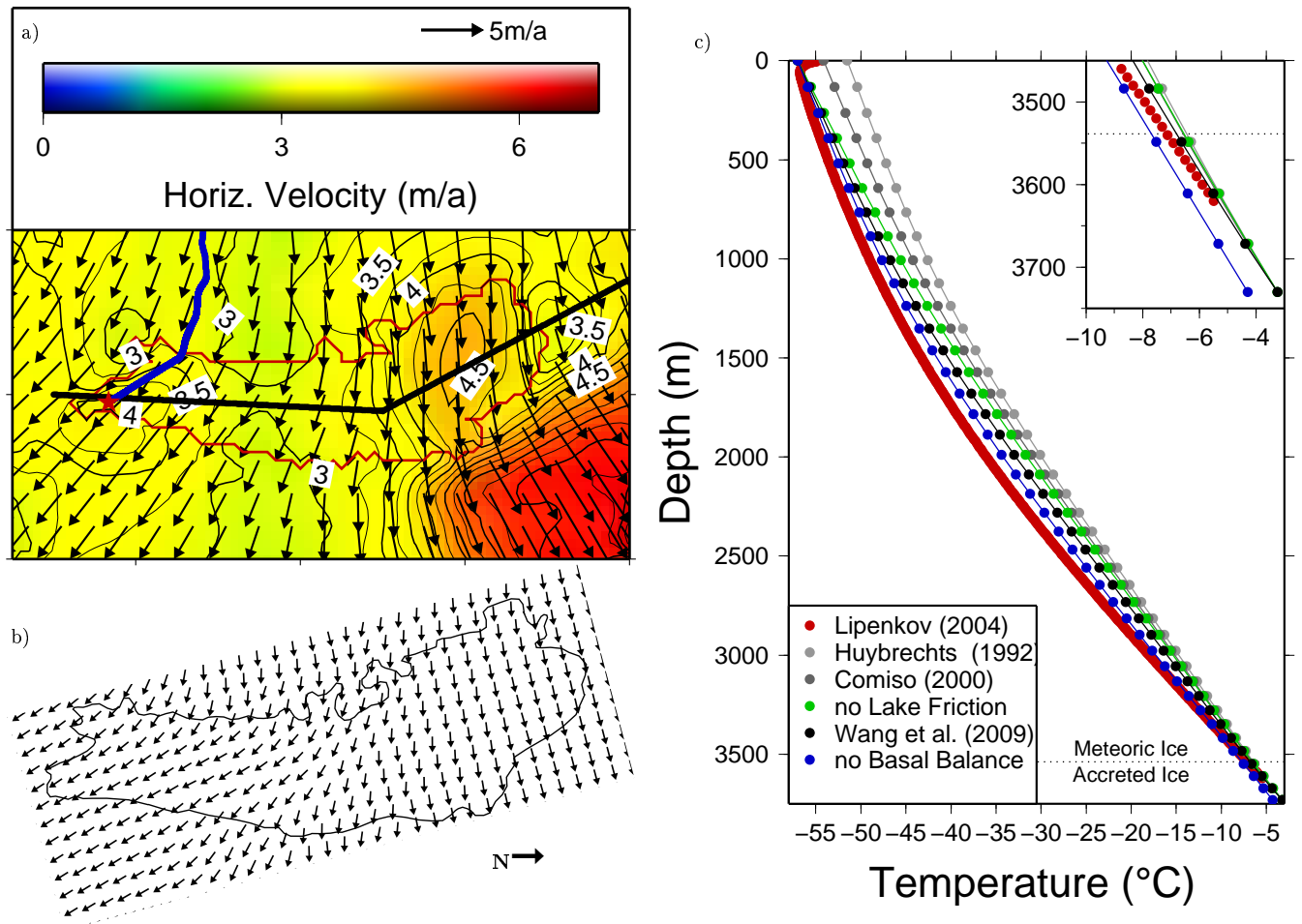


Fig. 4. a) Modelled averaged horizontal velocities for surface temperatures according to Wang and Hou (2009). The red line indicates the lake boundary, the blue line the *Vostok flow line* from Salamatin and others (2009) ending at Vostok Station (red star). The black line is the position of a temperature cross section. b) Flow field direction according to Tikku and others (2004). c) Observed (Lipenkov and others, 2004) and modelled vertical temperature profiles according to different forcings near Vostok Station.

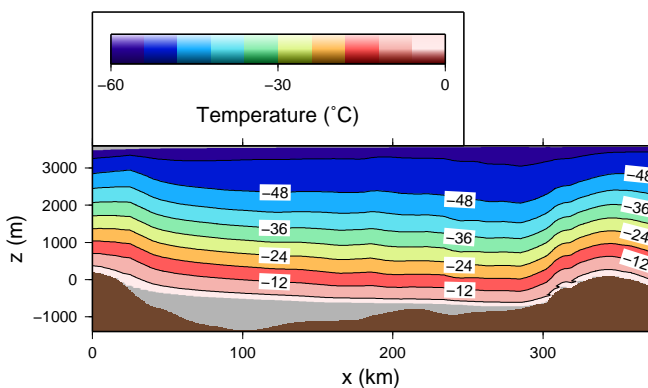


Fig. 5. Temperature cross section along the track shown in Figure 4a.

we consider the modelled flow- and temperature distribution sufficient under constant surface boundary conditions.

Impact of different forcings

We investigate the sensitivity of the ice flow above lake Vostok according to the impact of different boundary conditions, namely surface temperature, basal mass balance, and basal sliding. All parameters have significant impact on the ice flow regime. The impact of other boundary conditions, e.g.

geothermal heat flux and accumulation on the ice dynamics, are not investigated in this study.

Surface Temperature

A modified surface temperature field has a significant impact on the velocity, in particular in the already fast flowing areas of the northern and southern part of the lake itself, as well as north-east of the lake (Figures 6a-b and 7a-b). Compared to the reference forcing (Wang and Hou, 2009), the surface temperatures according to Huybrechts (1992) and Comiso (2000) are about 5°C and 2°C warmer, respectively (comp. Figure 7a-b). Hence the temperature dependent viscosity decreases, which corresponds with a velocity increase for these warmer surface temperature forcings. In addition, both warmer surface forcings induce a stronger southward deflection of the flow over the lake.

Basal mass balance

To investigate the influence of the basal mass balance on the flow regime, we present results with neglected basal melting and freezing above the lake in Figures 6c and 7c. The spatially varying basal mass balance has a heterogeneous impact on the flow. Basal freezing in the south (comp. Figure 2c) induces upward vertical velocities. Hence the ice is warmer in regions of freezing. In contrast, basal melting in the north results in downward advection of colder surface ice; consequently the ice is colder in this region compared to the control

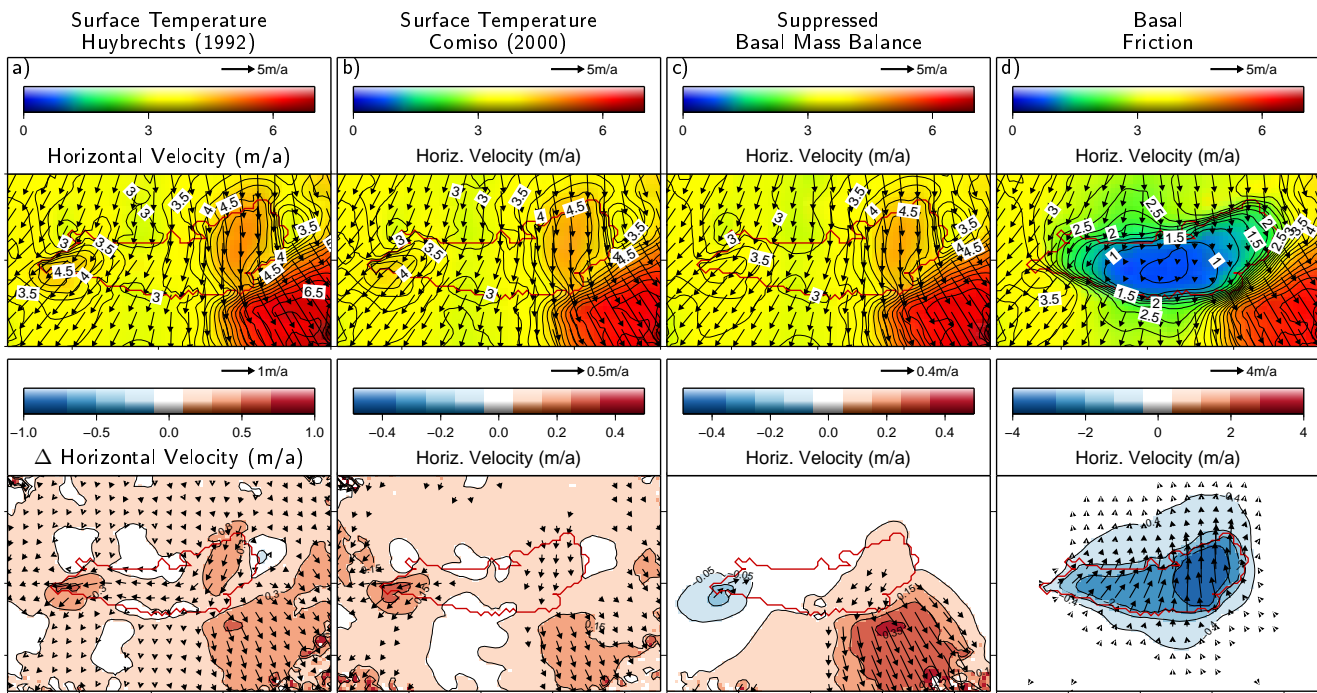


Fig. 6. Modelled mean horizontal velocities (top) and differences between this and the reference model (bottom; Figure 4a for surface temperature forcings according to a) Huybrechts (1992) and b) Comiso (2000), as well as for c) a model with suppressed basal mass balance at the lake-ice interface and d) a model with basal friction at the lake-ice interface.

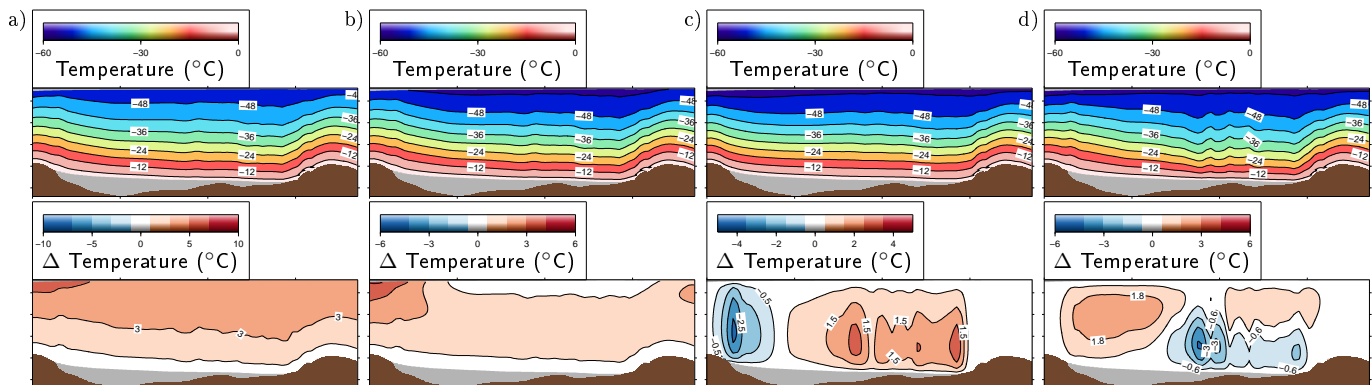


Fig. 7. Modelled temperature profile along the track indicated in Figure 4a across Vostok Subglacial Lake (upper panel) and differences between this and the reference model (lower panel, Figure 4c) for the same model forcings as in Figure 6a-d.

run. Note that for consistency Figures 6c and 7c indicate the effect of the *ignored* basal mass balance; hence the effect of the varying basal mass balance itself has the opposite sign. The modelled velocity (Figures 6c) is again closely linked to the temperature-dependent viscosity. Therefore, freezing in the south increases the velocity and intensifies the southward deflection of the flow. In contrast, the extended melting in the north reduces the horizontal velocity. Both effects have a significant impact on the downstream flow far beyond the lake's edge. In summary, the spatially varying basal mass balance pattern intensifies the flow divergence above lake Vostok.

Basal sliding

If basal sliding at the lake-ice interface is ignored, the reduced surface gradient over the lake significantly decreases the flow velocity (Figure 6d) in this diagnostic model setup. However, this effect is not limited to the lake itself. In particular, a significant (> 0.5 m/a) velocity decrease is modelled upstream. We conclude that subglacial lakes influence the ice flow in

the order of the lake's dimension. The reduced horizontal flow results in a longer transition time of the ice across the lake. This explains the twofold impact on the temperature (Figure 7d). First, basal freezing (in the south) and melting (in the north) modifies the vertical velocity. This results in advection of warmer ice upwards and colder ice downwards, as discussed in the previous section. Second, the relatively warmer surface temperatures (compared to upstream) result in a slight warming of the upper part of the ice column even in the north. This warming counteracts the freezing-induced cooling of the lower part of the ice column.

IMPACT OF A COUPLED ICE SHEET – LAKE SYSTEM

The basal-mass-balance boundary condition (Figure 2c) is derived from the model output of the lake-flow model ROMBAX (compare page 2), which is partly forced by the heat flux into the overlying ice sheet. Until now this was assumed to be con-

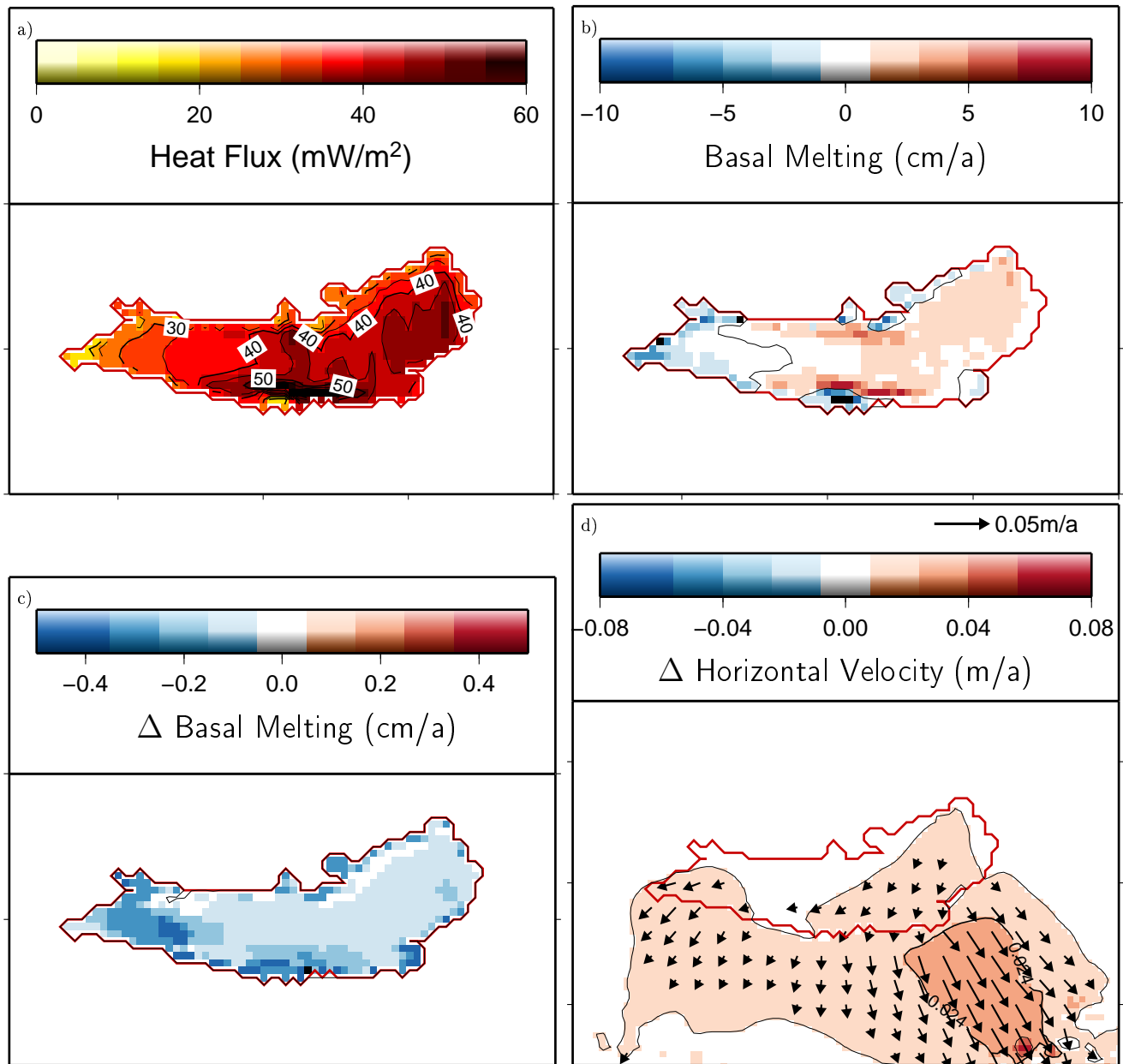


Fig. 8. a) Heat flux into the ice sheet, according to the output of the ice model RIMBAY, applied as an input boundary condition for the lake-flow model ROMBAX. b) Basal mass balance boundary condition for the ice flow model RIMBAY according to the coupled system and c) difference between Figure 2c and 8b). d) Difference between the vertically averaged horizontal flow of the uncoupled (Figure 4a) and the coupled model (slightly extended map to demonstrate the downstream effect).

stant 33 mW/m^2 where ice melts and zero where ice freezes (Thoma and others, 2008b). However, coupling of ROMBAX with the ice-flow model RIMBAY permits to model the exchange parameters *heat flux into the ice* and *basal mass balance* between both numerical models in a consistent way. From the modelled temperature profile within the ice above Vostok Subglacial Lake (Figure 5) the heat flux into the ice can be estimated according to $Q_{\text{Ice}} = c_p \cdot dT/dh$, with the thermal conductivity of ice $c_p = 2.1 \text{ W/(K m)}$ (Paterson, 1994) and the temperature gradient at the ice base. This results in a spatially varying heat-flux pattern with an average of 38.9 mW/m^2 as input for the lake-flow model ROMBAX (Figure 8a) and subsequently in a refined basal mass balance as input for the ice-flow model RIMBAY (Figure 8b-c). A detailed description of the coupling procedure is presented in Thoma and others (2010a).

In general, the increased heat flux into the ice results in a decrease of the melting area by 7% (from about $1.15 \cdot 10^4 \text{ km}^2$ to $1.07 \cdot 10^4 \text{ km}^2$) and an increase of the freezing area by 35% (from $5.28 \cdot 10^3 \text{ km}^2$ to $7.12 \cdot 10^3 \text{ km}^2$, Figure 8b,c). Consequently, the total basal melting reduces from $0.0910 \text{ km}^3/\text{a}$ to $0.0177 \text{ km}^3/\text{a}$, leading to slightly warmer basal ice. However, the flow field changes only slightly by the interactive coupling of the ice- and lake-flow model. The ice flow increases by less than about 0.5% (Figure 8d) above the lake and in its vicinity.

DISCUSSION

The recent view of basal processes at the base of the Antarctic Ice Sheet suggests a widespread occurrence of liquid water (e.g., Pattyn, 2010; Bell and others, 2011). This water drains into subglacial topographic depressions, indicated by more

than 370 subglacial lakes. With our coupled modelling approach, we explicitly calculate the response of the ice flow on melting and freezing in the area of Vostok Subglacial Lake. The interaction between subglacial lakes and the Antarctic Ice Sheet has clear consequences for the ice dynamics. The increased flow velocity due to lubrication at the bed and the impact of melting and freezing on the thermodynamics are of great importance. Our model results indicate that the ice flow velocity is significantly increased downstream of the lake, too. In general, basal freezing increases the ice temperature by the upward advection of accreted ice at the pressure melting point. Compared to regions of no basal freezing, this warming results in a significant decrease of the ice viscosity. (According to Paterson, 1994, p.97, the flow parameter A is modified by about 25% if we assume an average temperature of $T \approx -30^\circ\text{C}$ and a deviation of $\Delta T \approx 2^\circ\text{C}$). Hence the ice flow in warmer areas is slightly more decoupled from the surrounding flow field and the local surface gradient gains more relevance for the flow direction. On the other hand, ice sheet models, which neglect basal processes, misinterpret the impact of basal temperature because basal melting cools the ice while basal freezing leads to higher ice temperatures. We strongly suggest to improve the treatment of subglacial hydrology in further model investigations. A prognostic version of the presented model might indicate that only the consideration of the complex basal mass balance pattern at the lake-ice interface is able to maintain the observed southward surface slope across Vostok Subglacial Lake, which would otherwise level (Pattyn and others, 2004). Interaction of ice sheets with subglacial water systems is not limited to subglacial lakes. But in the transition zone between ice sheets and ice shelves (the grounding line), this interaction plays a crucial role, too (e.g. Vieli and Payne, 2005; Schoof, 2007; Docquier and others, 2011; Favier and others, 2011). In a future study we will expand our model to address these effects at the grounding line and over the ice shelves and ice rises as well.

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