

Satellite-based modeling of permafrost temperatures in a tundra lowland landscape

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Abstract

Remote sensing offers great potential for detecting changes of the thermal state of permafrost and active layer dynamics in the context of Arctic warming. This study presents a comprehensive feasibility analysis of satellite-based permafrost modeling for a typical lowland tundra landscape in the Lena River Delta, Siberia. We assessed the performance of a transient permafrost model which is forced by time series of land surface temperatures (LSTs) and snow water equivalents (SWEs) obtained from MODIS and GlobSnow products. Both the satellite products and the model output were evaluated on the basis of long-term field measurements from the Samoylov permafrost observatory. The model was found to successfully reproduce the evolution of the permafrost temperature and freeze-thaw dynamics when calibrated with ground measurements. Monte-Carlo simulations were performed in order to evaluate the impact of inaccuracies and in model forcing and uncertainties in the parameterization. The sensitivity analysis showed that a correct SWE forcing and parameterization of the snow's thermal properties are essential for reliable permafrost modeling. In the worst case, the bias in the modeled permafrost temperatures can amount to 5 °C. For the thaw depth, a maximum uncertainty of about ± 15 cm is found due to possible uncertainties in the soil composition.

Keywords: Permafrost modeling, Thermal state of permafrost, Thaw depth, MODIS, Land surface temperature, GlobSnow

1. Introduction

Satellite-based earth observation has become an indispensable tool for the investigation of climate change especially in remote areas such as the Polar regions (Hall, 1988). For most of the cryosphere components such as glaciers, ice sheets, sea ice, and snow cover satellite monitoring and change detection has been established for several decades (e.g. Stroeve et al., 2007; Armstrong and Brodzik, 2001; Rignot and Thomas, 2002). Although permafrost is one of the largest components of the Arctic cryosphere, satellite-based monitoring schemes do not exist. Nevertheless, numerous ecosystem processes of the Arctic are directly or indirectly related to the thermal state of permafrost and the freeze-thaw dynamics of the upper most soil (active) layer (Van Everdingen, 1998). This is especially true for the energy, water, and carbon cycles which are strongly determined by sub-surface processes that often operate on spatial scales below the grid spacing of atmospheric models (Wania et al., 2009a,b). If satellite-based permafrost monitoring can provide an improved spatial resolution, this would strongly improve the impact assessment of climate change in the Arctic (ACIA, 2004; AMAP, 2011). In addition, an operational scheme could be beneficial for risk analysis for infrastructure such as roads, pipelines, and buildings which are directly affected by the thermal stability of permafrost (Larsen et al., 2008).

One of the biggest challenges is that permafrost is a subsurface thermal phenomenon which cannot be directly observed by remote sensing techniques. Thus, current approaches of permafrost monitoring make use of surface indicators such as vegetation cover (Stow et al., 2004), geomorphological units, or combinations of different surface features (Panda et al., 2010) in order to infer information about the permafrost conditions. However, these methods can only provide a qualitative measure of the thermal state of permafrost and changes are only detected when there is an impact on the surface. The application of land surface temperature (LST) records measured by satellites such as MODIS in order to retrieve freeze-thaw degree days is proposed by Hachem et al. (2009). In principle, such LST time series can be used to force a transient permafrost model that is able to reproduce the full thermal dynamics of the ground as proposed by Marchenko et al. (2009). Further studies suggest that the quality as well as the spatial and temporal resolution of MODIS LST products would be sufficient for permafrost modeling in non-mountainous terrain (Langer et al., 2010; Westermann et al., 2011b). However, model approaches are always subject to numerous assumptions,

38 limitations, and uncertainties resulting from e.g. neglected processes and
39 uncertainties in the forcing data or parameter settings (Boike et al., 2012b).
40 Especially the soil and snow properties such as water/ice content, thermal
41 conductivity, heat capacity, and density are usually unknown which intro-
42 duce large uncertainties in heat flow calculations (e.g. Goodrich, 1982; Rinke
43 et al., 2008; Gouttevin et al., 2012).

44 This study provides a proof-of-concept for a satellite-based permafrost
45 monitoring and assesses its performance for a typical low land tundra site in
46 NE Siberia. We (i) perform a thorough validation for the employed satellite
47 data at the study site, (ii) present a thermal permafrost model forced by
48 satellite data that delivers soil temperature and thaw depth, and (iii) evaluate
49 the performance of the scheme and provide a sensitivity analysis for uncertain
50 model parameters and inaccurate forcing data.

51 **2. Validation site**

52 The study site is located in Northern Siberia on Samoylov Island (72.4° N;
53 126.5° E) in the Lena-River Delta (Fig. 1). The local climate is described as
54 arctic-continental with a mean annual air temperature (MAAT) of about
55 -13°C and a large annual air temperature amplitude ranging from about
56 -45°C in winter to 20°C in summer (Boike et al., 2012a). The total annual
57 precipitation is about 200 mm of which about 25% falls as snow during winter
58 (Boike et al., 2008; Langer et al., 2011a). The polar night lasts from the mid
59 of November to end of January and polar day lasts from the beginning of
60 May until the beginning of August. Samoylov Island features a typical tun-
61 dra landscape underlain by continuous permafrost. The permafrost reaches
62 depths of about 200 m (Grigoriev, 1960) and features relatively cold temper-
63 atures of about -9°C at the depth of zero annual amplitude (20 m) (Boike
64 et al., 2012b). However, temperature observations indicate strong changes
65 in the thermal state of permafrost which shows a steady warming of about
66 1°C between 2006 and 2011 at a depth of about 10 m (Boike et al., 2012a).

67 Samoylov Island belongs to an alluvial river terrace (Schwamborn et al.,
68 2002) elevated about 20 m above the normal river water level. The lower
69 western part of the island constitutes a modern floodplain which is frequently
70 flooded during ice break-up of the Lena River during spring. The validation
71 site of this study is located on the elevated river terrace mainly characterized
72 by moss and sedge vegetated tundra (Fig. 1). In addition, several lakes and
73 ponds occur which make up about 25% of the surface area of Samoylov Is-

74 land (Muster et al., 2012). The land surface of the island features the typical
75 micro-relief of polygonal patterned ground caused by frost cracking and sub-
76 sequent ice-wedge formation (Lachenbruch, 1962). The polygonal structures
77 usually consist of depressed centers which are surrounded by elevated rims.
78 The polygonal structures often occur in different stages of degradation with
79 partly to completely collapsed rims. The soil in the polygonal centers usually
80 consists of water saturated sandy peat with the water table standing close
81 to or above the surface (Langer et al., 2011a). The elevated rims are usually
82 covered with a dry moss layer underlain by wet sandy peat soils featuring
83 massive ice wedges. The volumetric water/ice content of the peat soils typi-
84 cally ranges from 60 to 80%. The volumetric mineral content is reported to
85 range from 20 to 40% while the volumetric organic content is on the order of
86 5 to 10% (Kutzbach et al., 2004; Zubrzycki et al., 2012). This cryogenic soil
87 complex reaches depth of 10 to 15 m and is underlain by sandy to silty river
88 deposits. The Lena River deposits are reported to reach depths of at least
89 1 km in the delta region (Grigoriev et al., 1996).

90 3. Methods

91 3.1. Model description

92 This study makes use of a 1D soil heat transfer model capable of rep-
93 resenting the freeze-thaw cycle and a dynamic snow cover formation and
94 ablation. The model is based on solving the heat transfer equation including
95 a term which accounts for the phase change of soil water (Yershov, 1998),

$$\left(C_h + \rho_w L_{sl} \frac{\partial \Theta_w}{\partial T} \right) \frac{\partial T}{\partial t} - \frac{\partial}{\partial z} \left(K_h \frac{\partial T}{\partial z} \right) = 0, \quad (1)$$

96 where T is the soil temperature, C_h the volumetric soil heat capacity and K_h
97 the soil thermal conductivity. $\frac{\partial \Theta_w}{\partial T}$ is the change of liquid soil water content
98 with temperature which in combination with the latent heat of fusion L_{sl} and
99 the density of water ρ_w gives the rate of energy turnover related to soil water
100 phase change. The volumetric soil heat capacity C_h can be calculated as
101 sum of heat capacities of each soil component C_j weighted by its volumetric
102 fraction Θ_j

$$C_h = \sum_j \Theta_j C_j, \quad (2)$$

103 where j represents each soil component (ice, water, mineral, and organic).
104 The soil thermal conductivity K_h is based on a modified version of the

105 deVries-model (De Vries, 1952) applicable in frozen or partly frozen soils,
 106 which has been successfully employed in permafrost modeling (Westermann
 107 et al., 2011a; Weismüller et al., 2011). The soil heat conductivity K_h is then
 108 calculated as

$$K_h = \frac{\sum_j \Theta_j f_j K_j}{\sum_j \Theta_j f_j}, \quad (3)$$

109 where f_j summaries soil specific parameters including shape factors for soil
 110 particles and threshold values for soil water circulation. A more detailed
 111 description of the parameterization can be found in Campbell et al. (1994).
 112 The volumetric content of liquid soil water with temperature $\Theta_w(T)$ is the
 113 freeze curve of the soil and strongly depends on soil composition and struc-
 114 ture. This soil specific freeze curve can be parametrized by a second order
 115 polynomial as

$$\Theta_w(T) = \begin{cases} \Theta_{w(\min)} + \frac{\Theta_{w(\max)} - \Theta_{w(\min)}}{1 - aT + bT^2} & \text{for } T < 0 \\ \Theta_{w(\max)} & \text{for } T \geq 0 \end{cases}, \quad (4)$$

116 where a and b are empirical factors, whereas $\Theta_{w(\max)}$ and $\Theta_{w(\min)}$ are the
 117 maximum and minimum liquid water content, respectively.

118 For the numerical solution of the model, the heat transfer equation (Eq. 1)
 119 is discretized spatially with finite differences. The time derivatives are solved
 120 using an ordinary differential equation solver (ode15s) provided by MATLAB
 121 which uses a self-adaptive time integrator and is well suited for stiff problems
 122 (Shampine and Reichelt, 1997).

123 3.2. Model setting, boundary conditions, and initialization

124 The model is solved on a soil domain ranging from 0 to 600 m depth
 125 containing 104 vertical grid cells. The size of the grid cells increases with
 126 depths with a minimum grid cell spacing of 2 cm at the surface and maximum
 127 spacing of 20 m at the bottom. The uppermost soil layer can take any soil
 128 composition, whereas the ground below 20 m depth is assumed to consist of
 129 fluvial sediments with uniform composition (cp. Sect. 2). Following literature
 130 values for sandy river deposits, the composition of the fluvial sediments is set
 131 to a mineral soil with 20% pore space which is fully saturated by water or
 132 ice (Boike et al., 2012a). The compositions of the soil grid cells between the
 133 variable surface layer and the static deep soil layers are linearly interpolated.
 134 Note that the applied model is limited to heat transfer in soils. Hence, the
 135 thermal dynamics underneath water bodies such as lakes is not represented

136 in the applied scheme. An additional layer of 60 grid cells with a constant
 137 grid cell spacing of 2 cm is stacked on top of the soil domain to represent the
 138 snow cover. The model is forced at the upper boundary by the land surface
 139 temperature LST where the surface is defined as the soil-atmosphere or the
 140 snow-atmosphere interface, respectively. As snow depth changes over time,
 141 the location of the upper boundary can be shifted dynamically on the snow
 142 grid (more detailed description in Westermann et al. (2011a)). For simplicity,
 143 the snow cover is treated as an effective snow cover with uniform and constant
 144 properties over depth and the entire simulation period. Following Goodrich
 145 (1982) the volumetric heat capacity of snow is calculated from the snow
 146 density ρ_s as

$$C_s = 2.09 \times 10^3 \rho_s. \quad (5)$$

147 At the lower boundary of the soil domain, a constant geothermal heat flux
 148 Q_{geo} is applied. Global heat flow data are available through the International
 149 Heat Flow Commission (IHFC) (Pollack et al., 1993). We apply the geother-
 150 mal heat flux value of 0.053 Wm^{-2} which is measured in a 600 m borehole
 151 close to Tiksi located about 140 km east of our field site.

152 3.3. Model forcing

153 The forcing dataset consists of a synthesized time series of land surface
 154 temperatures (LST) and snow water equivalents (SWE) (Fig. 2). The entire
 155 forcing dataset covers a period from 1982 to 2011 which is divided into a
 156 target period ranging from 2002 to 2011 and a spin-up period from 1982
 157 to 2001. During the target period, the forcing of the permafrost model is
 158 exclusively based on remote sensing data including the MODIS LST, MODIS
 159 snow cover fraction (SFC), and GlobSnow SWE products. The spin-up of
 160 the model starts from an initial temperature field of the soil domain which
 161 is calculated assuming steady state heat flow with a constant average soil
 162 surface temperature $T_{0(\text{av})}$. The 20 year spin-up period allows to start with
 163 a transient temperatures distribution down to a depth of the approximately
 164 20 m. During the spin-up period, the surface temperature forcing is obtained
 165 from ERA-Interim reanalysis data, whereas SWE data are obtained from
 166 GlobSnow.

167 3.3.1. Surface temperature

168 During the spin-up period (1982-2001) satellite-based land surface tem-
 169 perature (LST) measurements from MODIS are not available. Therefore,

170 the required surface temperature forcing is extracted from the ERA-Interim
171 reanalysis product provided by the European Centre for Medium-Range
172 Weather Forecasts (ECWMF). The ERA-Interim product contains the full
173 set of forecast and analyzed fields of a numerical weather model within which
174 numerous meteorological observations are assimilated (Dee et al., 2011). The
175 reanalysis product provides four time daily gridded surface temperatures
176 since 1979 with a spatial resolution of 0.5° . The ERA-Interim product is
177 extensively validated and found to be in good agreement with meteorological
178 observations (e.g. Simmons et al., 2010; Szczypta et al., 2011; Mooney et al.,
179 2011). In contrast to the earlier version ERA-40, ERA-Interim is reported
180 to provide reliable temperature values in the Arctic (Screen and Simmonds,
181 2011). The coarse scale surface temperature values of the reanalysis product
182 are interpolated to the location of the study site using bicubic interpolation.

183 During the target period (2002-2011) the surface temperature forcing is
184 based on the MODIS L3 collection 5 LST products MOD11A1 (Terra) and
185 MYD11A1 (Aqua) with a spatial resolution of 1 km. The used LST products
186 contain day- and night-time surface temperatures which are obtained and ra-
187 diometrically corrected by the generalized split window approach (Wan and
188 Dozier, 1996). From the daily tiles a time series of daily LST averages is
189 compiled for the pixel encompassing the validation site. Frequent data gaps
190 occur due to clouds resulting in a clustered time series with an overall data
191 availability of 68%. The clustered LST time series leads to a systematic over-
192 representation of surface temperatures during clear sky conditions which can
193 cause a cold bias during winter (Westermann et al., 2012). A number of stud-
194 ies have addressed the difficulties associated with clustered LST data when
195 used to derive long-term LST averages (Hachem et al., 2009; Langer et al.,
196 2010; Westermann et al., 2011b). However, missing data are filled by linear
197 interpolation in order to obtain a continuous data record from which weekly
198 LST averages are inferred. In addition to overrepresented clear sky LST val-
199 ues, erroneously measured cloud top temperatures can cause a cold-bias in
200 the LST averages during summer and winter (Liu et al., 2010; Westermann
201 et al., 2012). Despite the admixture of free water surfaces within the MODIS
202 pixel, the obtained LST data are considered to represent the surface temper-
203 ature of the land or the snow cover as appropriate. The fraction of free water
204 surface within the MODIS pixel is approximately 25% (cp. Sect. 2). In addi-
205 tion, strong sub-resolution land surface heterogeneities can occur during the
206 snow melt period due to persistent snow patches (Westermann et al., 2011b).
207 However, field observations indicate that this period is relatively short (2 - 3

208 weeks) at the study site.

209 3.3.2. Snow cover

210 The GlobSnow product provides longterm data on snow water equivalent
211 (SWE) and snow extent (SE) across the northern hemisphere since 1979.
212 GlobSnow is a hybrid product which assimilates passive microwave satellite
213 measurements, as well as records from climate stations to derive daily SWE
214 maps with a spatial resolution of 25 km (Takala et al., 2011). The SWE
215 retrieval algorithm has been developed and validated by the Finnish Mete-
216 orological Institute (FMI) for various tundra and alpine landscapes (Luoju
217 et al., 2010). The average error of the GlobSnow SWE product is reported
218 to be less than 35 mm and even smaller for tundra landscapes. However,
219 extensive field studies demonstrate that passive microwave SWE detection
220 is subject to large uncertainties mainly introduced by the snow morphology,
221 vegetation cover, and the presence of white (refrozen and bubble rich) ice on
222 lakes and rivers (Foster et al., 2005; Derksen et al., 2005, 2011). Largest re-
223 trieval errors are reported to occur during snow cover accumulation and melt.
224 A comprehensive overview on satellite based snow cover monitoring and the
225 potential error sources is given by Frei et al. (2012). The grid cell containing
226 the validation site contains approximately 60% land surfaces similar to that
227 of the validation site, 20% river arms, and 20% floodplains. Despite this
228 sub-resolution landscape heterogeneity, the grid cell is considered represen-
229 tative for the validation site. This is especially critical during snow fall and
230 snow melt when large spatial differences in snow cover can occur between the
231 different landscape units.

232 In order to reduce the discrepancies in spatial resolution between MODIS
233 LST (1 km) and GlobSnow SWE (25 km), additional snow cover information
234 is obtained from the MODIS snow cover products (MOD10A1, MYD10A1).
235 Among other information, the tiles contain daily snow cover fractions (SCF)
236 at a spatial resolution of 500 m. The satellite data are available during the
237 entire target period (2002-2011) and are provided by the National Snow
238 and Ice Data Center (NSIDC) (Hall and Riggs, 2007). The MODIS snow
239 cover detection algorithm is based on the Normalized Difference Snow Index
240 (NDSI) including a consistency check based on the surface temperature (Hall
241 et al., 2002). The MODIS snow product is extensively validated for different
242 landscape types (e.g. Salomonson and Appel, 2004; Stroeve et al., 2006; Hall
243 et al., 2009). Similar to the LST product, uncertainties are introduced by
244 erroneous cloud detections which potentially leads to data loss and overesti-

245 mated SCF values (Hall and Riggs, 2007). Data gaps due to clouds are filled
246 by linear interpolation and weekly SCF averages are compiled afterwards.
247 The MODIS SCF product provides high-resolution data on timing of snow
248 cover build-up and disappearance. These additional information are used to
249 enhance the GlobSnow SWE product which is subject to errors especially
250 during the snow accumulation and ablation periods. A stable snow cover is
251 expected to occur when two consecutive weeks feature snow cover fractions of
252 larger than 10%. GlobSnow SWE values are set to zero when the stable snow
253 cover criterium is not fulfilled. Conversely, linear interpolation between the
254 onset of a stable snow cover and the first non-zero SWE value is applied when
255 a stable snow cover is indicated by MODIS SCF but not by GlobSnow SWE.
256 The enhanced SWE time series is validated by SWE field observations and
257 continuous snow depth measurements at the validation site (cp. Sect. 3.4).

258 *3.4. Validation data sets*

259 All forcing data are validated by surface temperature and snow depth
260 measurements at the study site which are continuously available since 2002.
261 The surface temperatures are calculated from measurements of a down fac-
262 ing long wave radiation sensor (CG1, Kipp & Zonen, Netherlands). The
263 out going long wave radiation is converted to surface temperature by using
264 Stefan-Boltzmann law assuming the surface emissivity to be unity. Under
265 specific meteorological conditions this simplification can lead to overesti-
266 mated surface temperatures (Westermann et al., 2011b). However, it is the
267 best available estimate on the radiometric surface temperature as measured
268 by MODIS and calculated by ERA-Interim. Snow depth measurements for
269 a point on Samoylov Island are performed by an ultra sonic ranging sensor
270 (SR50, Campbell Scientific, USA) located close to the surface temperature
271 measurements.

272 The performance of the model is validated by comparing the simulated
273 soil temperatures to a 5 year record of ground temperatures measured in a
274 borehole in 2.5 m and 11 m depth. The borehole is located close to the me-
275 teorological station. The area around the borehole is characterized by low
276 centered polygons featuring dry rims and wet centers (cp. Sect. 2). Within
277 a distance of more than 100 m only two polygonal ponds occur with surface
278 areas less than 80 m². The borehole is equipped with a temperature chain
279 (XR-420, RBR Ltd., Canada) which features an absolute accuracy of about
280 0.05 °C. The validation depths are well suited to investigate the model per-
281 formance for the annual temperature cycle and the longterm temperature

282 evolution. The borehole temperatures have been recorded with 1 h resolu-
283 tion since July 2006. In addition, manual thaw depth measurements are
284 used in order to validate the modeled thaw dynamics. Thaw depth measure-
285 ments have been performed since 2002 on a weekly basis on a 500 m² plot
286 consisting of a regular grid of 150 measurement points. The thaw depth is
287 measured relative to the surface using a metal rod. These measurements are
288 consistently available throughout the end of July, which is therefore used as
289 reference date for the thaw depth validation. Prior to the model validation
290 all required parameters are obtained by fitting the model to the borehole
291 temperature measurements. This set of parameters is also used as midpoint
292 for the following Monte-Carlo simulations (cp. Sect. 3.5).

293 *3.5. Monte-Carlo simulations*

294 Monte-Carlo simulations are performed in order to evaluate the sensitivity
295 of the permafrost model to (i) uncertainties in the selected model paramete-
296 rers (in particular soil and snow thermal parameters) and (ii) inaccuracies in
297 the forcing data. The uncertainties and the inaccuracies propagate through
298 the model and result in uncertainties in the simulated soil temperatures and
299 thaw depths. Different magnitudes and combinations of uncertainty ranges
300 and accuracy levels are evaluated based on 24 Monte-Carlo simulations (cp.
301 Tab. A.1) each of which involves 500 model realizations. For each model
302 realization, random variations in model forcing or parameterization are gen-
303 erated for the respective accuracy level and uncertainty class. The generation
304 of the random values follows a uniform probability distribution.

305 In a first series of simulations, only the uncertainties which are intro-
306 duced by the model parameterization are considered (Tab. A.1). We assume
307 different classes of uncertainty, in following denoted high, intermediate, and
308 low uncertainty. The parameters are grouped into three categories (snow,
309 soil, and initialization). We distinguish the following Monte-Carlo simula-
310 tions: High, intermediate, and low uncertainty for all parameter categories
311 (MCp1), high uncertainty for two of the categories and high, intermediate,
312 and low uncertainty for the remaining category (MCp2-4). This procedure is
313 applied in order to explore how much the output uncertainty can be reduced
314 by enhancing the knowledge of a single parameter group. The assumed high
315 uncertainty class for the snow parameters is in accordance with reported
316 variabilities of snow properties in the Arctic as summarized by Sturm et al.
317 (1997). Note that the thermal conductivity and density of the snow cover
318 are considered to be independent from each other in the specified ranges of

319 uncertainty. This assumption is made in order to represent the full range of
320 thermal conductivities ($0.03 - 0.2 \text{ Wm}^{-1}\text{K}^{-1}$) that is reported for densities
321 between 200 and 300 kgm^{-3} (Sturm et al., 1997). The high uncertainty class
322 assumed for the initial surface temperature $T_{0(\text{av})}$ equates to the variance of
323 the annual average surface temperature between 1979 and 1982 obtained from
324 the ERA-Interim dataset. The assumed variation of the freeze curve covers a
325 wide range of freeze characteristics from sandy to silty soils, as suggested by
326 field observations (Langer et al., 2011b). The high uncertainty class of the
327 soil components is assumed to realistically represent the potential variability
328 of low land tundra soils which can range from medium-dry organic soils to wa-
329 ter/ice saturated mineral soils (Boike et al., 2012a). For the soil constituents,
330 uniform probability distributions have been chosen with the constraint, that
331 the sum of all is unity. According to the applied conductivity model (cp.
332 Sect. 3.1), the uncertainties in soil composition correspond to uncertainties
333 in soil thermal conductivity (unfrozen soil) of about $\pm 0.33 \text{ Wm}^{-1}\text{K}^{-1}$ for
334 the high uncertainty class, $\pm 0.2 \text{ Wm}^{-1}\text{K}^{-1}$ for the intermediate uncertainty
335 class, and $\pm 0.15 \text{ Wm}^{-1}\text{K}^{-1}$ for the low uncertainty class. The uncertainties
336 in heat capacity are $\pm 0.8 \text{ MJm}^{-3}$, $\pm 0.4 \text{ MJm}^{-3}$, and $\pm 0.2 \text{ MJm}^{-3}$ respec-
337 tively. In frozen state, the uncertainties in thermal conductivity are more
338 than doubled. In contrast, the uncertainties in heat capacity are almost
339 three times smaller than in unfrozen state. In general, the uncertainties in
340 the soil thermal properties decrease with depth as the varying soil compo-
341 sition at the surface is linearly interpolated to a fixed composition in 20 m
342 depth (cp. Sect. 3.2).

343 The impact of inaccuracies in the LST and SWE forcing data on the
344 model results are considered in similar manner as for the parameterization
345 (Tab. A.1). The assumed low accuracy levels are in accordance with reported
346 accuracies for the data products (cp. Sect. 3.3). The accuracy of the forcing
347 data is then stepwise enhanced by a factor of two for the intermediate and
348 the high accuracy simulations. At first, the accuracies are enhanced for
349 both forcing datasets (LST and SWE) simultaneously (MCf1) and later for
350 LST and SWE individually (MCf2-3). In contrast to the settings for the
351 parameterization, the inaccuracy of the currently unprocessed forcing dataset
352 is set to zero. The inaccuracies in the SWE forcing do not affect the duration
353 of the snow cover which is considered to be accurately detected by the satellite
354 products. Hence, a minimum snow cover of 2 cm (corresponding to one snow
355 grid cell) is assumed when a snow cover is indicated by MODIS SCF but not
356 by GlobSnow SWE.

357 4. Results

358 4.1. Validation of the forcing data

359 Daily and weekly surface temperature values from MODIS LST and ERA-
360 Interim are compared with surface temperature averages obtained by radio-
361 metric measurements at the Samoylov field site (Fig. 3). Despite a spread
362 of about 5°C , there is a coherent relationship between the field measure-
363 ments and the MODIS data over the entire temperature range from -50 to
364 $+20^{\circ}\text{C}$. The data are mostly well centered around the 1:1 line. On average,
365 the temperature deviations between the MODIS LST data and the obser-
366 vations is about $\pm 2^{\circ}\text{C}$ which equates to an accuracy of about 3% relative
367 to the entire temperature range. However, at surface temperatures between
368 -10 and 10°C numerous outliers are observed. The outliers are consistently
369 negative and feature temperature offsets of up to 20°C . The ERA-Interim
370 surface temperatures show a lower spread in the range from -20 to 20°C .
371 However, under very cold conditions (below -20°C) the reanalysis prod-
372 uct shows a steadily increasing cold bias which reaches a maximum offset of
373 about 10°C at surface temperatures of about -40°C . From daily MODIS
374 LST values, weekly averages are generated after the gap filling procedure (cp.
375 Sect. 3.3.1). The outliers around the freezing point disappear after averag-
376 ing, but a slight cold bias of about 2°C emerges. The agreement between
377 ERA-Interim and field observations increases for weekly averages, but the
378 characteristic temperature bias below -20°C remains. However, extremely
379 low surface temperatures only occur occasionally so that temperature offsets
380 larger than 5°C are very rare.

381 The applied model scheme assumes constant and uniform snow properties
382 so that GlobSnow SWE data can be directly assigned to snow depths via the
383 snow density (cp. Sect. 3.3.2). A snow density of approximately 250 kg m^{-3} is
384 found by the fitting procedure (cp. Sect. 3.4) by which the evolution of snow
385 depth can be relatively well reproduced (Fig. 4). The fitted snow density is
386 well within the range of snow density measurements performed at the same
387 study site (Boike et al., 2012a). Using a constant snow density as a first
388 order approximation, the satellite data tend to underestimate snow depths
389 when the snow cover is relatively thick. However, differences in snow depth
390 between field observations and satellite data are in 90% of cases less than
391 5 cm. This equates to a SWE accuracy of $\pm 13\text{ mm}$ if a constant snow density
392 is applicable to the study site. Relative to the entire SWE range (0 - 150 mm)
393 at the study site, this corresponds to a relative accuracy of about 10%. Note

394 that a satellite product with a resolution of 25 km is compared to snow depth
395 measurements at a specific point and a perfect match can not be expected
396 since spatial snow cover differences are very likely due to wind drift and
397 micro topographic variations within the satellite footprint. In most cases,
398 the applied correction based on the MODIS SCF product leads to a slightly
399 better reproduction of the onset of snow accumulation. The uncorrected
400 GlobSnow data often show a delayed snow cover build up on the order of
401 about two weeks. In a few occasions, the MODIS SCF correction leads to an
402 earlier snow cover build up. In contrast to snow cover build up, the timing
403 of snow melt is consistent between the GlobSnow and the MODIS product
404 so that a correction does not occur. In general, the timing of snow melt is
405 well reproduced by the satellite data.

406 *4.2. Model performance and uncertainty*

407 The model performance with regard to temperature is shown in Fig. 5 for
408 soil depths of 2.5 and 11 m. The solid line indicates the result of the best pa-
409 rameter setting found after the fitting procedure (cp. Sect. 3.4). At a depth
410 of 2.5 m the general magnitude of the annual temperature dynamics can be
411 relatively well reproduced. However, a constant cold bias of about -1°C is
412 found for the best fit results during summer. During winter, the temperature
413 differences between the model results and the borehole measurements can be
414 as large as 2°C , but strongly vary in magnitude and sign. After winter, a
415 short delay in the rewarming of the soil occurs in the simulations. However,
416 the timing of soil cooling after summer is mostly in good agreement with
417 the observations. Compared to the measurements, the simulated tempera-
418 tures in 11 m depth are slightly too cold. The temperature offset increases
419 from about 0.5 to 1°C with the largest temperature differences during sum-
420 mer. Hence, the measured soil warming exceeds the simulations, but the
421 model reproduces a general soil warming over the entire target period. Fig. 5
422 also displays the results of MCp1 (cp. Tab. 1) according to the prescribed
423 classes for low, intermediate, and high uncertainty. An almost symmetric
424 range of uncertainty around the median occurs around the best fit for the
425 low uncertainty class. At 2.5 m depth the output uncertainty is about $\pm 1^{\circ}\text{C}$
426 during summer and $\pm 3^{\circ}\text{C}$ during winter, whereas at 11 m depth the output
427 uncertainty is almost constant at around $\pm 1^{\circ}\text{C}$. The width of the uncer-
428 tainty range slightly increases over the target period. For the intermediate
429 uncertainty class, the summertime temperature uncertainty remains almost
430 centered around the best fit but the range increases to $\pm 2^{\circ}\text{C}$. In some oc-

431 casions a slightly negative temperature shift of the uncertainty field can be
432 observed. In contrast, a clear positive temperature shift occurs during win-
433 ter so that the output uncertainty ranges with -4°C and $+5^{\circ}\text{C}$ around the
434 best fit. In fact, a constant positive shift of the uncertainty fields occurs at
435 a depth of 11 m ranging with -1.5°C and $+2^{\circ}\text{C}$ around the best fit. As
436 in the previous uncertainty class, the width of the uncertainty range slightly
437 increases over the target period. In the high uncertainty class, the output un-
438 certainty strongly increases. At 2.5 m depth the uncertainty spreads around
439 the best fit with -3°C and $+2^{\circ}\text{C}$ during summer and -3°C and $+13^{\circ}\text{C}$
440 during winter. The strong deviation is attributed to a strongly delayed re-
441 freezing of the active layer. At a depth of 11 m the uncertainty field ranges
442 with -2°C and $+4.5^{\circ}\text{C}$ around the best fit at the beginning of the target
443 period. The upper limit of the uncertainty range increases by about 0.5°C
444 while the lower limit stays almost constant in the course of the target period.
445 In both depths, the measured soil temperatures mostly stay within the limits
446 of the low uncertainty class.

447 A comparison of measured and simulated thaw depths at the end of July is
448 shown in Fig. 6. The thaw depth measurements show a large spatial scatter
449 with a range of up to 30 cm. In most years, the distribution of the thaw
450 depth is symmetric with about 50% of the values located within half of the
451 range. The simulated thaw depths for the best fit are always within the
452 range of the measurements. The difference between the median of the thaw
453 depth measurements and the simulated (best fit) thaw depth is in most cases
454 lower than 10 cm. The model usually tends to overestimate thaw depths.
455 However, main features of the inter-annual thaw dynamics are to some extent
456 reproduced by the model. In particular, the relatively large thaw depth in
457 2005 which decreases again in 2006 and the comparatively low thaw depth
458 2009 followed by a sharp increase in 2010. With low input uncertainty, the
459 resulting thaw depth uncertainty is smaller than ± 5 cm. The uncertainty
460 bar is usually centered around the best fit. In some cases, however, the
461 best fit is located at the upper edge of the uncertainty range. Since only
462 completely thawed soil grid cells are considered in the uncertainty analysis,
463 it is possible that the upper limit of the uncertainty range is underestimated
464 at maximum by 2 cm. With intermediate input uncertainty, the uncertainty
465 in thaw depth increase to about ± 8 cm and reaches its maximum of about
466 ± 15 cm in the high uncertainty class. The maximum uncertainty range agrees
467 in magnitude with the observed thaw depth variability. In most cases, the
468 uncertainty range is larger for years with deeper thaw depth.

469 *4.3. Uncertainty due to model parameters*

470 As shown in Sect. 4.2, the uncertainties of the input parameters lead to
471 a large spread in the soil temperature calculations. The distributions of
472 the average soil temperatures in 2.5 m and 11 m depth as revealed from the
473 Monte-Carlo simulations are displayed in Fig. 7. In each MC simulation, the
474 input uncertainty of one parameter group is stepwise reduced down to a fixed
475 (best fit) value with zero uncertainty (cp. Sect. 3.5). The temperature dis-
476 tributions at maximum uncertainty are similar for the different simulations
477 indicating a sufficient number of model runs. Almost all simulations show
478 positively skewed distributions in both depth with a stronger temperature
479 spread in 2.5 m than in 11 m depth. The positive skewness indicates that
480 strong temperature biases occur more frequently in positive than in negative
481 direction which is attributed to the delayed refreezing caused by the phase
482 change of soil water. The median of the high uncertainty class is located
483 at about -9.5°C for all simulations and both depth. This is about 0.5°C
484 colder than expected from the best fit average. This negative bias from the
485 expected best fit value is decreased by reducing the uncertainty in the soil
486 parameters. For all other simulations the bias between the median and the
487 best fit value remains. However, reducing the uncertainty in the soil pa-
488 rameters does not affect the spread of the distributions which stays almost
489 constant. Conversely, lowering the uncertainty in the snow parameters leads
490 to a strong reduction in the temperature spread. Furthermore, the simula-
491 tions with reduced uncertainty in snow reveal a much lower skewness. The
492 bias between soil temperature measurements and best fit simulation might
493 still be explained by the lowest snow uncertainty. The temperature distri-
494 bution becomes completely symmetrical when zero uncertainty for the snow
495 parameters is assumed. However, a temperature spread of about $\pm 1^{\circ}\text{C}$ re-
496 mains due to the uncertainties in the other parameter groups. Variations in
497 the uncertainty of the initial conditions only show a minor impact on the
498 resulting temperature distribution.

499 In summary, the results demonstrate that the uncertainties in modeled
500 soil temperatures are most strongly determined by uncertainties in the snow
501 parameters. Snow cover uncertainties not only control the temperature
502 spread but also the shape of the distribution. The effect of the snow thermal
503 conductivity on the thermal state of permafrost is much more pronounced
504 than that of the snow density which controls heat capacity and depth of the
505 snow cover.

506 The sensitivity of the modeled thaw depths to uncertainties in the param-
507 eterization is exemplarily displayed for the year 2010 (Fig. 8). As discussed
508 in Sect. 4.2, the maximum input uncertainty in the parameterization results
509 in a thaw depth uncertainty of about ± 15 cm. The thaw depth distributions
510 are positively skewed with the median thaw depth about 5 cm lower than ex-
511 pected from the best fit. Reducing the uncertainty in the parameter groups
512 reveals that the spread in thaw depth, the skewness of the distribution, as
513 well as the bias between median and best fit result are entirely governed by
514 the soil parameters. The snow cover as well as the initial surface tempera-
515 ture barely affect the simulated thaw depths. When the uncertainty of the
516 soil parameters is reduced the uncertainty in thaw depth decreases almost
517 proportional. However, a spread in thaw depths of about +10 cm and -5 cm
518 remains even when the soil parameters are fixed at the best fit values. Under
519 the given environmental conditions (external forcing, thermal state of the
520 ground) the contribution of the freeze curve to the thaw depth uncertainty is
521 almost negligible. The spread in the spatially distributed thaw depth mea-
522 surements is almost similar to the spread of the modeled thaw depths. Hence,
523 the variance of soil properties at the study site is well represented by the high
524 uncertainty class.

525 4.4. *Uncertainty due to forcing data*

526 The sensitivities of the model to potential inaccuracies in the LST and
527 SWE forcing data are illustrated in Fig. 9 and Fig. 10. Assuming a low accu-
528 racy in LST and SWE leads to a strong spread in the resulting temperature
529 distributions in both depths (Fig. 9). In contrast to the temperature distri-
530 butions which result from uncertainties in the parameterization, the distri-
531 butions according to the different accuracies in the forcing data are almost
532 uniform and centered around the best fit value. A stepwise enhancement of
533 the accuracy by a factor of two leads to an almost proportional decrease in the
534 temperature spread. However, the bias between the temperature measure-
535 ments and the best fit simulation is within the margins of the high accuracy
536 level. The spread of the temperature distribution strongly decreases when
537 inaccuracies in the SWE data are neglected. Close to the surface (2.5 m),
538 the observed temperature spread equates approximately to the correspond-
539 ing LST accuracy. The temperature distribution at low LST accuracy reveals
540 a positive skewness which disappears for the high accuracy level. The tem-
541 perature spread caused by inaccuracies in LST decreases with depth (11 m)
542 while the shape of the distributions remains the same. A similar behavior can

543 be observed for the results of the SWE simulations. However, the resulting
544 temperature spread is by a factor of four larger compared to the distributions
545 obtained from the LST simulations. The bias between measured soil tem-
546 peratures and the best fit simulation can be already explained with a high
547 accuracy (± 10 mm) in the SWE forcing.

548 The uncertainty in the modeled thaw depth is less than ± 10 cm for the
549 lowest accuracy level of the combined LST and SWE simulation (Fig. 10).
550 For the higher accuracy levels, the uncertainty in thaw depth spreads only
551 in negative direction. The median of the uncertainty distribution equates
552 always to the thaw depth which is calculated in the best fit model run.
553 The simulations show that inaccuracies in the SWE forcing only marginally
554 contribute to the uncertainties in thaw depth.

555 **5. Discussion**

556 *5.1. Applicability of the forcing data*

557 Extensive validation of the MODIS LST data reveals that despite out-
558 liers and frequent data gaps a reliable forcing dataset of weekly surface tem-
559 peratures can be generated from the satellite measurements. The observed
560 quality of the MODIS LST data is comparable to accuracies reported for
561 other polar regions (Koenig and Hall, 2010; Hachem et al., 2012). Similar
562 to a MODIS validation study performed on Svalbard (Westermann et al.,
563 2012), a lower quality of the LST data is observed for temperatures around
564 the freezing point. However, the general data quality seems to be better at
565 our study site which is most likely related to the lower cloudiness because
566 of the more continental climate conditions. Hence, it can be assumed that
567 the quality of a surface temperature forcing generated from MODIS LST
568 strongly varies in different climate regions. In addition to that, it must be
569 assumed that the LST quality varies throughout the annual cycle. With-
570 out ground observation and validation, we estimate a maximum accuracy
571 of ± 2 °C for the generated LST forcing. With such an LST accuracy, the
572 thermal state of permafrost is reproduced within a range of $+1.5$ and -1 °C
573 in 11 m depth. The skewness of the simulated temperature range indicates
574 that LST biases have a stronger impact in positive than in negative direction
575 which is most likely caused by the thermal insulation of the snow cover and
576 the delayed refreezing due to the phase change of soil water (Goodrich, 1982;
577 Romanovsky and Osterkamp, 2000; Smith et al., 2010). Inaccuracies in the
578 LST forcing are especially critical during summer when they are not overlain

579 by the inaccuracies in the SWE forcing or uncertainties in the snow cover
580 parametrization. Hence, inaccuracies in the LST forcing directly affect the
581 quality of thaw depth simulations. With an LST accuracy of $\pm 2^\circ\text{C}$ the thaw
582 depth is reproduced with an uncertainty of about $\pm 3\text{ cm}$.

583 The SWE forcing generated from the GlobSnow and MODIS SCF prod-
584 ucts reproduces the evolution of the snow depth at the study site relatively
585 well by assuming a constant snow density. The combination of both snow
586 cover products provides a better reproduction of the onset of snow cover.
587 Comparing the simulated and the measured soil temperatures reveals tem-
588 perature differences especially during winter which are most likely attributed
589 to a wrong representation of the insulating effect of the snow cover. This can
590 result from either incorrect SWE forcing, or inappropriate snow parameteri-
591 zation, or a combination of both. The MC simulations reveal a very strong
592 impact of SWE inaccuracies on the model performance. The highest ac-
593 curacy level assumed in the MC simulations for the SWE forcing equates
594 approximately to the observed accuracy after calibration of the snow density
595 with field measurements (cp. Sect. 4.1). The thermal state of permafrost
596 is reproduced with an uncertainty of about $\pm 2.5^\circ\text{C}$ with a SWE accuracy
597 of about $\pm 10\text{ mm}$. This is still below the performance that can be reached
598 with a realistic LST accuracy of about $\pm 2^\circ\text{C}$. However, a much lower SWE
599 accuracy level ($\pm 40\text{ mm}$) must be considered in regions with sparse weather
600 stations (Luoju et al., 2010) and when field measurements are not available
601 for calibration. Our results show that realistic permafrost simulations with
602 a transient heat transfer model would be almost impossible with such low
603 accuracies in the SWE forcing. In contrast to the permafrost temperatures,
604 the thaw depths are found to be more or less independent from the SWE
605 accuracy. However, this might be different in regions where the permafrost
606 temperature is already close to the freezing point as observed by Åkerman
607 and Johansson (2008). In any case, the impact of snow on the active layer
608 dynamics can be very complex and dependent on regional factors (Zhang,
609 2005). The performed sensitivity study demonstrates that a highly accurate
610 snow cover forcing is crucial for reliable permafrost modeling.

611 *5.2. Applicability of the model scheme*

612 The results of this study demonstrate that permafrost modeling in low
613 land tundra based on remote sensing data is in principle possible, provided
614 that a correct snow cover forcing is available. A fairly simple model scheme
615 with very coarse approximations on soil strata, snow cover properties, and

616 neglected soil water flow reasonably reproduces the temperature and freeze-
617 thaw dynamics at the study site over a period of 5 years. In addition, the
618 observed warming of deeper permafrost at the study site could be reproduced.
619 Note that the borehole temperatures that are used for validation represent
620 the specific thermal state at one point of the study site which is unlikely to
621 be exactly reproduced by the generalized soil parameterization of the model.
622 Hence, it can not be expected that the model exactly reproduces the bore-
623 hole measurements. However, the best fit result of this study is comparable
624 in accuracy to other model studies which usually use in situ measurements
625 as forcing data and feature more optimization possibilities due to a more
626 complex parametrization (e.g. Jiang et al., 2012). The synthesized dataset of
627 soil surface temperature and snow water equivalent has a reasonable quality
628 in order to be used as forcing for a permafrost model (cp. Sect. 5.1). Despite
629 the relatively good performance during summer, the applied scheme reveals
630 shortcomings especially during the winter period. On one hand it is possible
631 that the temperature mismatches between model and observations are at-
632 tributed to inaccuracies in the SWE forcing (cp. Sect. 5.1), but on the other
633 hand it is very likely that they are related to the static representation of the
634 thermal snow properties. The applied scheme does not account for the natu-
635 ral dynamics of the snow cover which passes through several stages of meta-
636 morphisms depending on temperature, moisture, compaction, wind drift, and
637 interactions with the underlying surface or vegetation (e.g. Colbeck, 1982;
638 Sturm et al., 2001). Due to these processes, the thermal conductivity of
639 the snow cover can change by an order of magnitude. Parameterizations
640 of snow thermal properties (e.g. Sturm et al., 1997) have not been exten-
641 sively validated for arctic regions and thus involve large uncertainties. The
642 performed sensitivity tests are based on reported variabilities of snow ther-
643 mal properties. The resulting uncertainty in the modeled soil temperature
644 clearly demonstrate the large impact of the snow properties on the thermal
645 state of permafrost. This is not only critical for satellite-based permafrost
646 modeling but involves permafrost modeling in general. A very recent study
647 demonstrates that the oversimplification of the snow thermal properties in
648 climate models strongly impacts the representation of permafrost and the
649 related soil-biological processes (Gouttevin et al., 2012). An oversimplified
650 snow cover parameterization becomes even more problematic as observations
651 indicate that the arctic snow cover has changed strongly over the last decades
652 and is expected to change even more pronounced in the future (Callaghan
653 et al., 2011; Derksen and Brown, 2012).

654 The performed sensitivity analysis takes into account a wide range of soil
655 types ranging from medium-dry organic soils to water/ice saturated mineral
656 soils. Within the applied model, this leads to strong variations in the soil
657 thermal properties of the upper meters (cp. Sect.3.5). The large impact
658 of the thermal conductivity of the uppermost organic soil layer on the re-
659 gional climate and the thermal state of permafrost has been demonstrated
660 in several studies (e.g. Rinke et al., 2008; Koven et al., 2009; Wisser et al.,
661 2011). However, our results show that the impact of uncertainties in the soil
662 thermal properties is largely overruled by the impact of uncertainties in the
663 snow thermal properties. This result can be considered valid for landscapes
664 that feature comparable subsurface and climate conditions and where similar
665 assumptions of uncertainty are applicable.

666 In contrast to the thermal state of permafrost which is almost entirely
667 governed by the snow cover, the active layer dynamic is mainly determined
668 by the soil composition. The uncertainty in modeled thaw depth is clearly
669 reduced when some knowledge about subsurface properties is available. This
670 is especially true for the soil water or ice content which mainly determines the
671 thaw depth. The use of further satellite products such as surface soil mois-
672 ture (e.g. Wagner et al., 2007), surface wetness classifications (e.g. Muster
673 et al., 2012), and freeze-thaw status (e.g. Bartsch et al., 2007) could help
674 to reduce the uncertainties in thaw depth simulations. However, the robust-
675 ness of the active layer dynamics towards uncertainties in the thermal snow
676 properties is misleading. The thermal state of permafrost and the active
677 layer dynamics are decoupled due to the very cold permafrost temperatures.
678 Previous studies show that due to the cold conditions, a large fraction of the
679 summertime ground heat flux is attributed to soil warming and a relatively
680 constant fraction is consumed by the thawing of ground ice (Langer et al.,
681 2011b). However, this could be different in the case of warmer permafrost
682 conditions when most of the ground heat flux can be used for thawing (Yer-
683 shov, 1998). Thus, a correct representation of the snow cover becomes critical
684 for active layer modeling when climate warming has potentially the greatest
685 impact on the thaw depth. The results of this study clearly demonstrate
686 that large challenges remain for operational permafrost modeling based on
687 satellite data especially in terms of snow cover forcing and parameterization.
688 Furthermore, we would like to point out, though, that the results of this
689 study are only applicable for regions with climate forcing and soil conditions
690 similar to those at the of study site in NE Siberia. In addition, the impact of
691 surface heterogeneities such as ponds or lakes on the thermal ground regime

692 is not accounted for and heat transfer due to soil water convection is not
693 included. Thus, further validation studies should be performed for a range of
694 different climate conditions and landscape types before compiling an opera-
695 tional product. In addition, further model development is necessary in order
696 to represent surface heterogeneities.

697 **6. Conclusions**

698 This study highlights the potential of permafrost monitoring using read-
699 ily available remote sensing products. A thermal permafrost model enables
700 reconstruction of the thermal state of the subsurface, which is not directly ac-
701 cessible through remote sensing. The scheme was able to reproduce the small
702 warming of permafrost temperatures of about 1 °C that has been measured at
703 about 10 m depth over the past 5 years at the study site. The thermal prop-
704 erties of the snow pack, and particularly its thermal conductivity, constitute
705 the largest source of uncertainty.

- 706 • The main features of permafrost dynamics, such as the inter-annual
707 variations in thaw depth and the decadal warming trend, can be mod-
708 eled from satellite data if the snow properties and soil compositions are
709 known.
- 710 • The accuracy of land surface temperature forcing obtained from MODIS
711 LST allows permafrost modeling with uncertainty ranges of less than
712 ± 2 °C in temperature and ± 3 cm in thaw depth. These uncertainties
713 are found to be much smaller than uncertainties induced by other fac-
714 tors such as SWE forcing and the thermal properties of the snow cover.
- 715 • The accuracy of GlobSnow SWE data appears to be adequate for rep-
716 resenting the evolution of the snow depth with an accuracy better than
717 ± 5 cm, provided that calibration data are available. This accuracy al-
718 lows permafrost modeling with a temperature uncertainty of less than
719 ± 3 °C. However, the specified accuracy of the GlobSnow product would
720 lead to large uncertainties of more than ± 5 °C.
- 721 • The largest uncertainties in permafrost modeling are induced by un-
722 known thermal properties of the snow cover. Reliable permafrost mod-
723 eling is not feasible in the absence of information on local snow cover
724 characteristics.

725 • Uncertainties in modeling the active layer dynamics are largely at-
726 tributed to uncertainties in soil compositions, especially the soil wa-
727 ter/ice content. In the worst case setting for the soil composition, the
728 thaw depth can be reproduced with an uncertainty of about ± 15 cm.

729 This permafrost monitoring scheme could be operationalized for per-
730 mafrost monitoring on a pan-arctic scale, provided the range of uncertainties
731 imposed by the model parameters and the available data are acceptable.

732 *Acknowledgements*

733 We thank Günther Stoof, Waldemar Schneider and our Russian partners
734 at AARI for the technical and logistical support of our field work. We grate-
735 fully acknowledge the financial support by the Helmholtz Association through
736 a grant (VH-NG 203) awarded to Julia Boike. Furthermore, the authors ac-
737 knowledge the financial support by the European Union FP7-ENV project
738 PAGE21 under contract number GA282700. We also like to thank Joel Row-
739 land and one anonymous reviewer for the very constructive comments which
740 helped to improve our manuscript.

Appendix A. Settings for Monte-Carlo simulations

Table A.1: Overview on the uncertainty settings for the different model parameters and forcing data in the performed Monte-Carlo simulations. The given uncertainty ranges refer to the parameterization of the best fit model run as mid point. The soil and freeze curve parameters are either volumetric fractions or parameters of the freeze curve (cp. Eq. 4).

	soil & freeze curve parameters				initialization		forcing			
	water Θ_w	mineral Θ_m	organic Θ_o	a b	min. liq. water $\Theta_w(\text{min})$	density ρ_s [kgm^{-3}]	snow conductivity K_s [$\text{Wm}^{-1}\text{K}^{-1}$]	$T_0(\text{av})$ [$^{\circ}\text{C}$]	LST [$^{\circ}\text{C}$]	SWE [mm]
Best. fit	0.60	0.35	0.05	20 4	0.03	247	0.11	-8.5	-	-
MCP1	± 0.2	± 0.2	± 0.2	± 10 ± 2	± 0.03	± 50	± 0.08	± 2	± 0	± 0
	± 0.1	± 0.1	± 0.1	± 5 ± 1	± 0.015	± 25	± 0.04	± 1	± 0	± 0
	± 0.05	± 0.05	± 0.05	± 2.5 ± 0.5	± 0.007	± 12.5	± 0.02	± 0.5	± 0	± 0
MCP2	± 0.2	± 0.2	± 0.2	± 10 ± 2	± 0.03	± 50	± 0.08	± 2	± 0	± 0
	± 0.1	± 0.1	± 0.1	± 5 ± 1	± 0.015	± 25	± 0.04	± 1	± 0	± 0
	± 0.05	± 0.05	± 0.05	± 2.5 ± 0.5	± 0.007	± 12.5	± 0.02	± 0.5	± 0	± 0
	± 0	± 0	± 0	± 0 ± 0	± 0	± 50	± 0.08	± 2	± 0	± 0
MCP3		± 0.2		± 10 ± 2	± 0.03	± 50	± 0.08	± 2	± 0	± 0
						± 25	± 0.04		± 0	± 0
						± 12.5	± 0.02		± 0	± 0
						± 0	± 0	± 2	± 0	± 0
MCP4		± 0.2		± 10 ± 2	± 0.03	± 50	± 0.08	± 2	± 0	± 0
								± 1	± 0	± 0
								± 0.5	± 0	± 0
								± 0	± 2	± 40
MCF1		± 0		± 0 ± 0	± 0	± 0	± 0	± 0	± 1	± 20
									± 0.5	± 10
									± 2	± 40
MCF2		± 0		± 0 ± 0	± 0	± 0	± 0	± 0	± 1	± 0
									± 2	± 0
									± 1	± 0
MCF3		± 0		± 0 ± 0	± 0	± 0	± 0	± 0	± 0.5	± 0
									± 2	± 40
									± 1	± 20

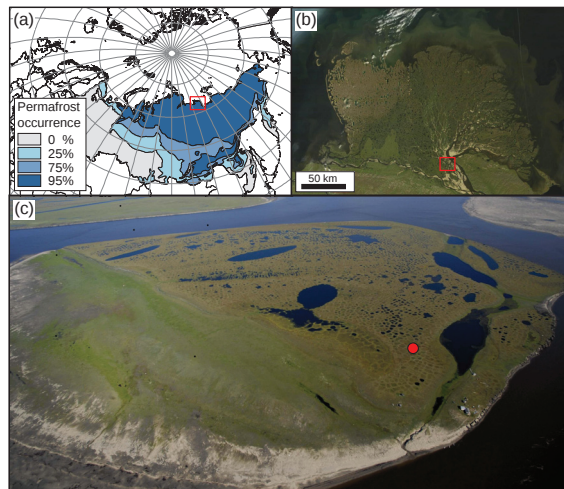


Figure 1: Location of the validation site on Samoylov Island. (a) Extent of permafrost in Russia with the location of the Lena River Delta marked with a red box (after Kotlyakov and Khromova, 2002). (b) MODIS (Terra) satellite image of the Lena River Delta obtained in August 2012 (NASA, 2012). (c) Aerial photograph of Samoylov Island featuring a surface area of about 4.5 km^2 . The location of the measurement site is marked with a red dot.

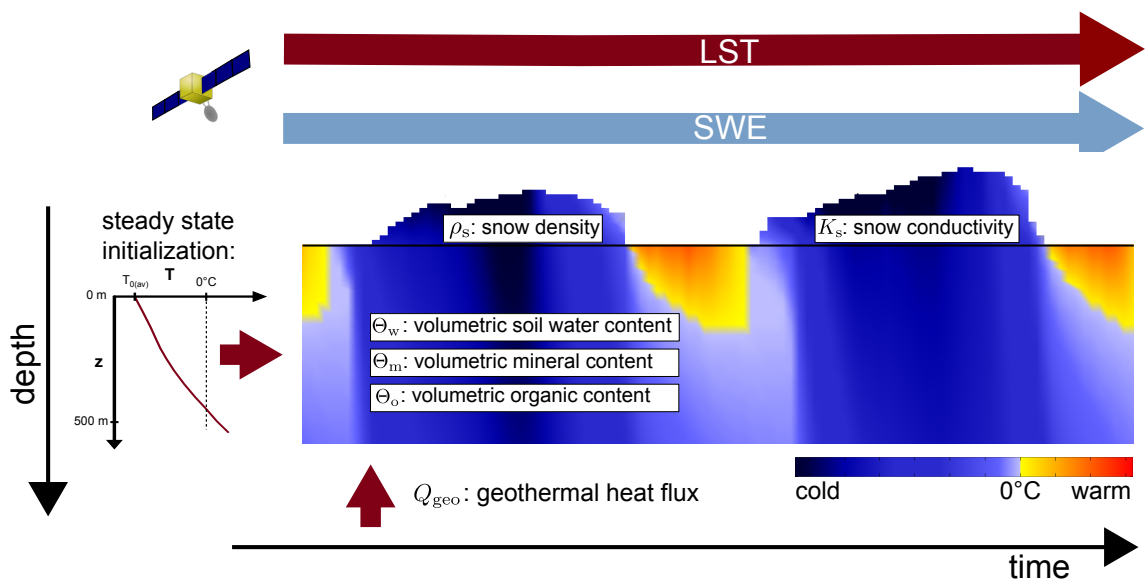


Figure 2: Scheme of the applied permafrost model with employed parameters. During the target period from 2002 to 2011, the model is forced solely by the MODIS LST, MODIS SCF, and GlobSnow SWE products. The model is run for 20 year spin-up period (1982-2001) prior to the target period during which the LST forcing is obtained from reanalysis data (ERA-Interim).

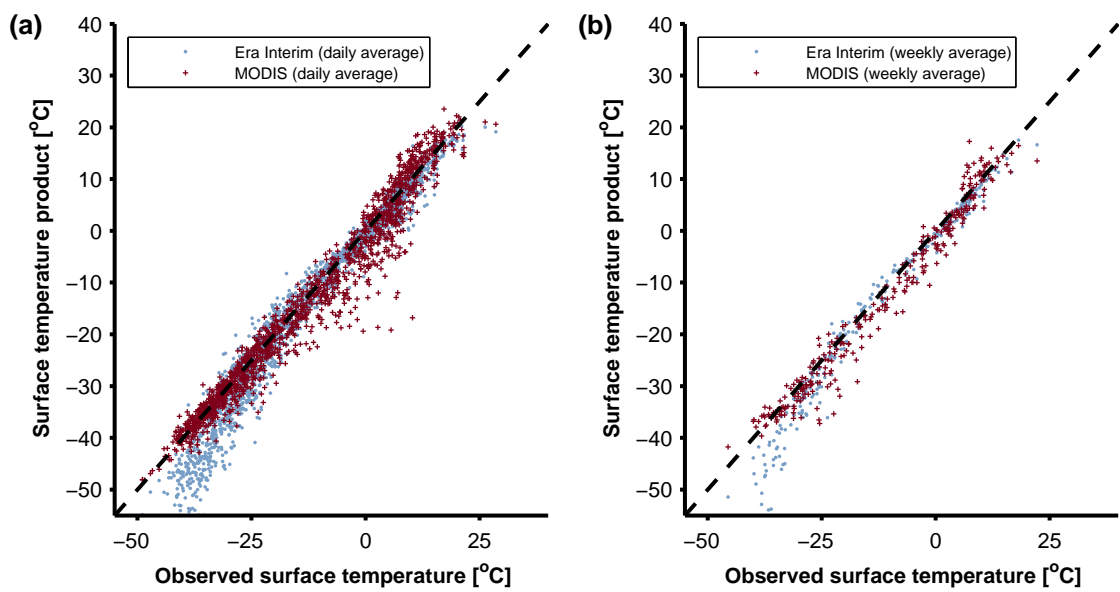


Figure 3: Comparison of daily (a) and weekly (b) surface temperature averages measured at the Samoylov field site with MODIS LST (MOD11A1, MYD11A1) and ERA-Interim LST values. The comparison includes field measurements from 2002 to 2011.

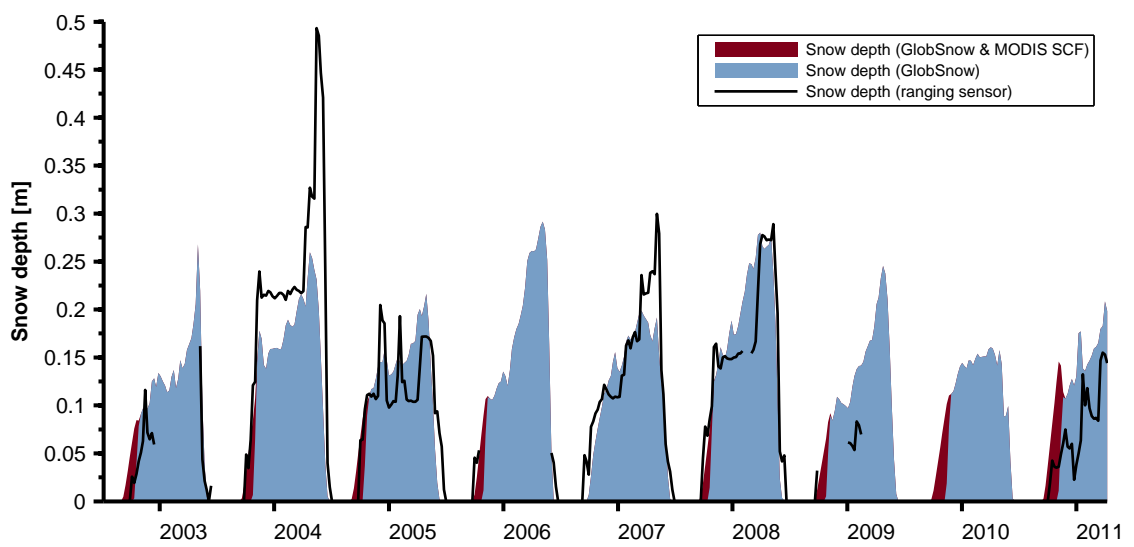


Figure 4: Snow depth evolution obtained from in situ measurements and GlobSnow SWE assuming a constant snow density of approximately 250 kgm^{-3} .

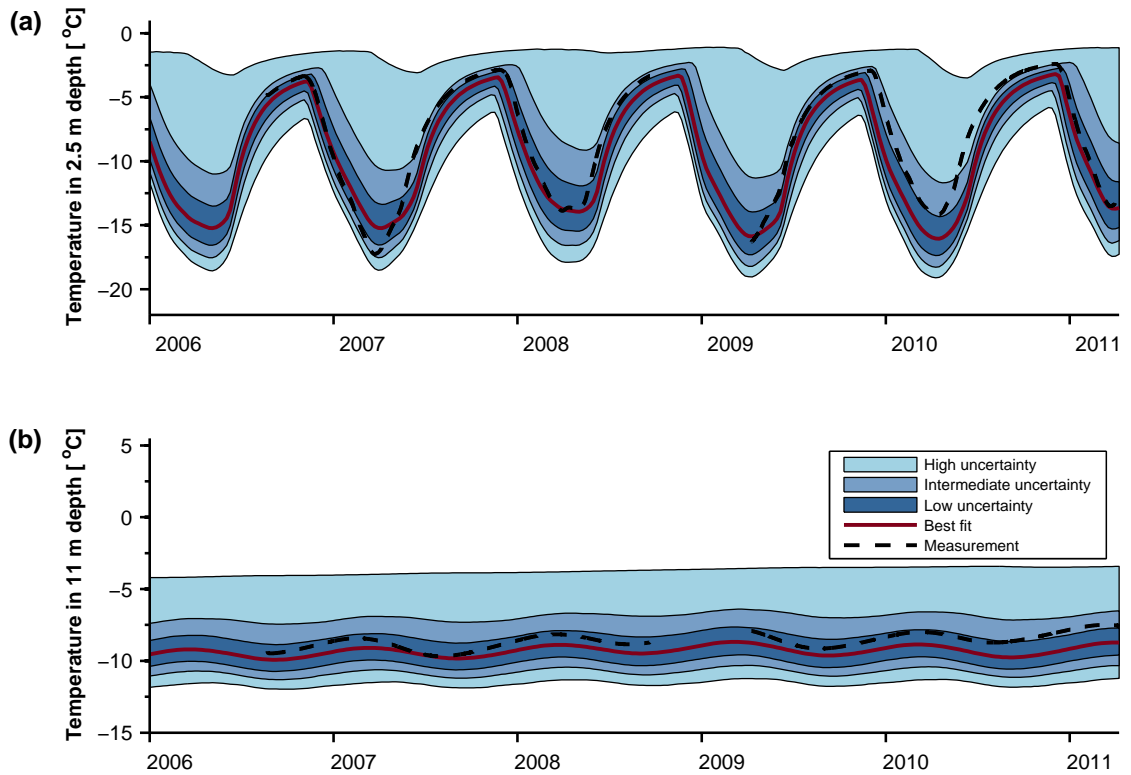


Figure 5: Comparing the results of the MCp1 (Tab. A.1) simulations with in-situ temperature measurements at (a) 2.5 m depth and (b) 11 m depth. The shaded areas illustrate the ranges of the resulting temperature distributions.

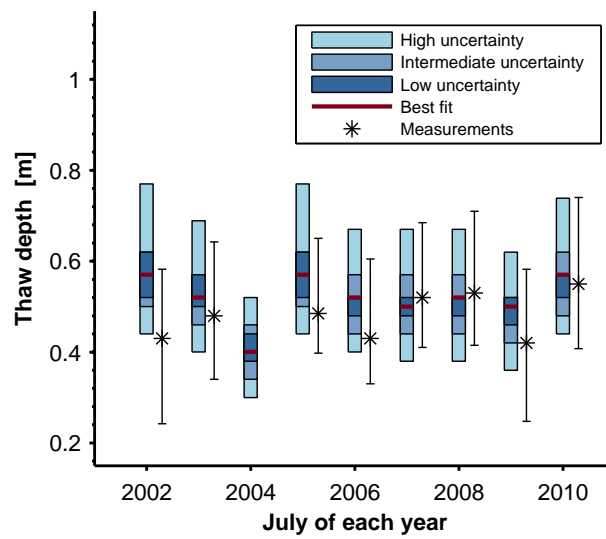


Figure 6: Measured versus modeled thaw depths at the end of July. The spatial variability of thaw depths at the study site are illustrated by the whiskers. The shaded bars show the ranges of thaw depths as resulted from the MCp1 simulations (Tab. A.1).

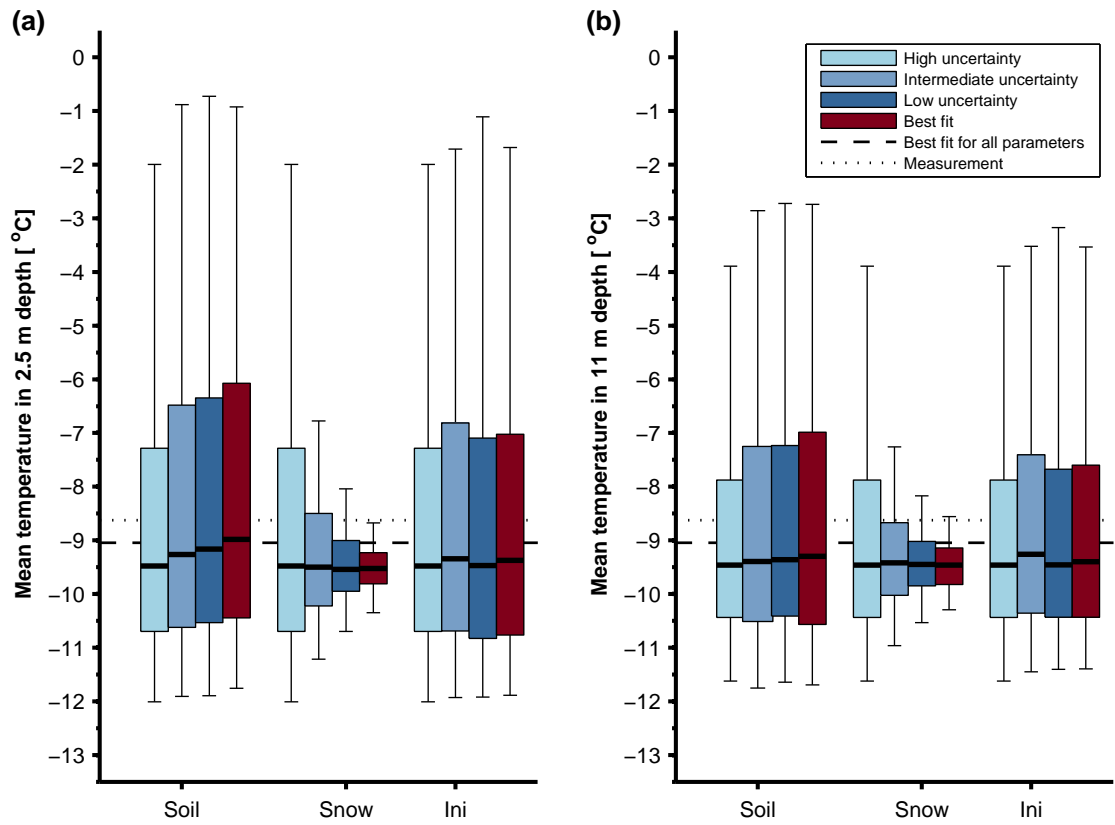


Figure 7: Uncertainty distributions of average permafrost temperatures modeled for a) 2.5 m and b) 11 m depth with different uncertainties on the soil, snow, and initialization (Ini) parameters (cp. MCp2-4 Tab.A.1). The permafrost temperatures are averaged over the validation period during which borehole temperature data are available. The shaded bars represent the quartile and the whiskers the range of the resulting temperature distributions.

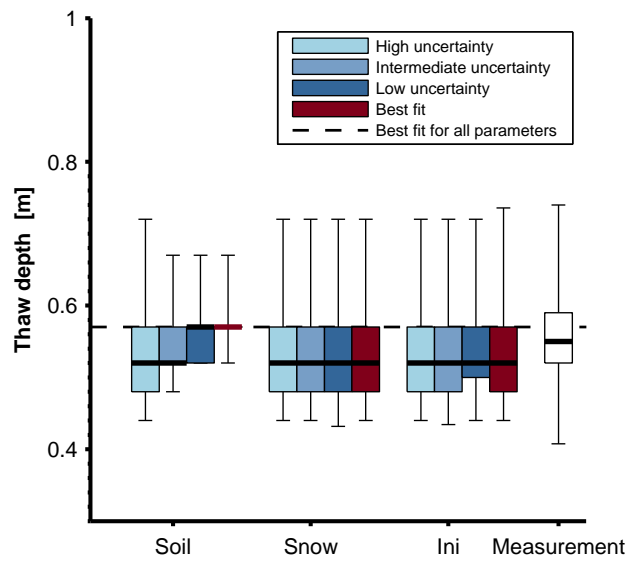


Figure 8: Uncertainties in modeled thaw depth associated with different ranges of uncertainty on the soil, snow, and initialization (Ini) parameters (cp. MCp2-4 Tab. A.1). The shown data depict maximum thaw depth in August 2010. The range of the thaw depth measurements reflects the spatial variability. The bars and whiskers represent the quartile and range of the thaw depth distributions.

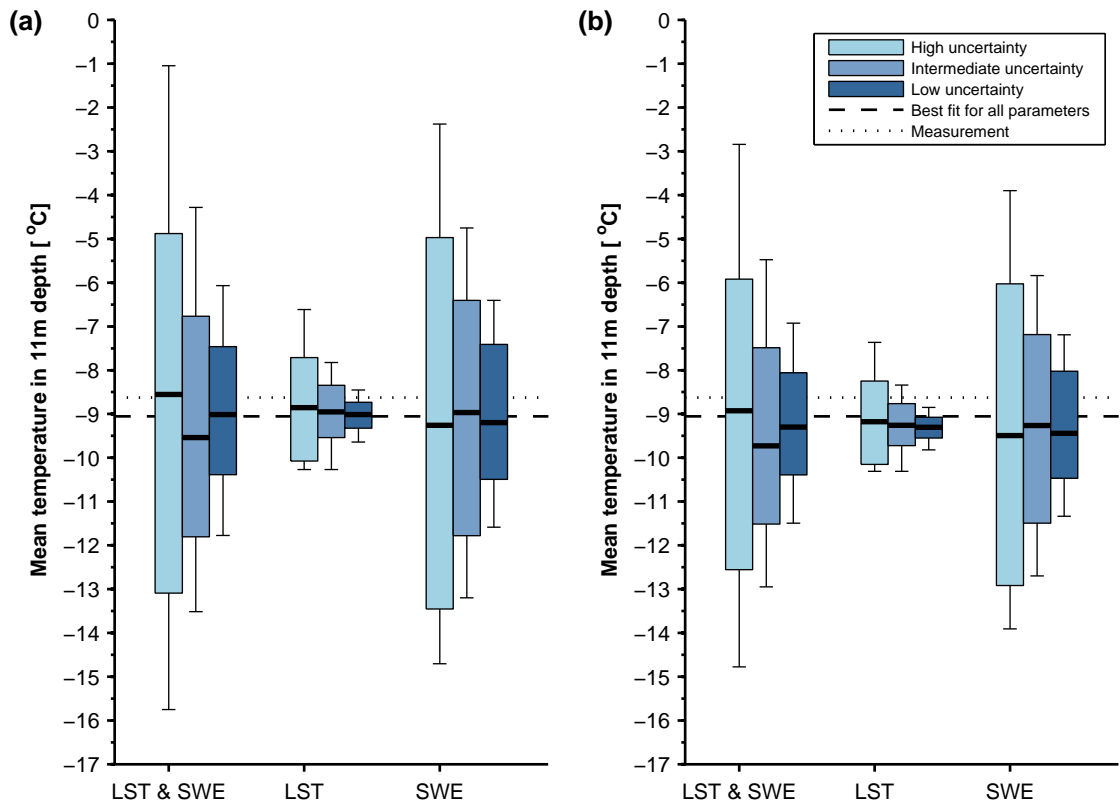


Figure 9: Uncertainty distributions of average permafrost temperatures modeled for a) 2.5 m and b) 11 m depth with different assumptions on accuracy in model forcing (cp. MCf1-3 Tab. A.1). The permafrost temperatures are averaged over the validation period during which borehole temperature data are available.

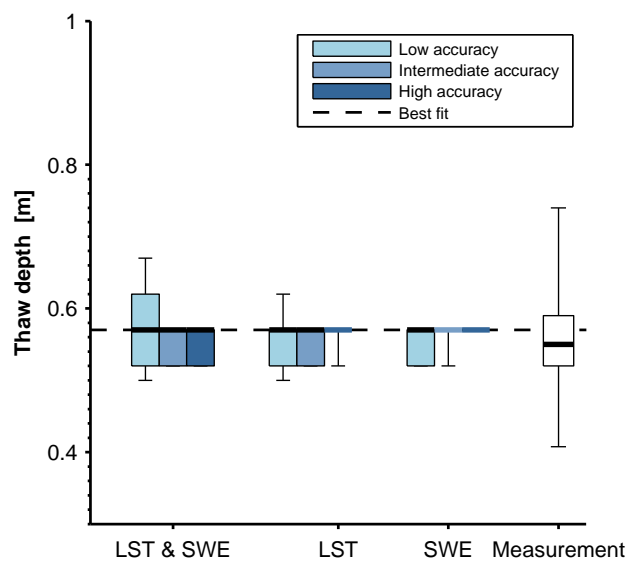


Figure 10: Uncertainties in modeled thaw depth associated with different levels of accuracy in model forcing (cp. MCf1-3 Tab. A.1). The shown data depict maximum thaw depth in August 2010. The range of the thaw depth measurements reflects the spatial variability.

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