

# Ensemble Data Assimilation for Coupled Models of the Earth System

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IGG, University of Bonn, September 27, 2019

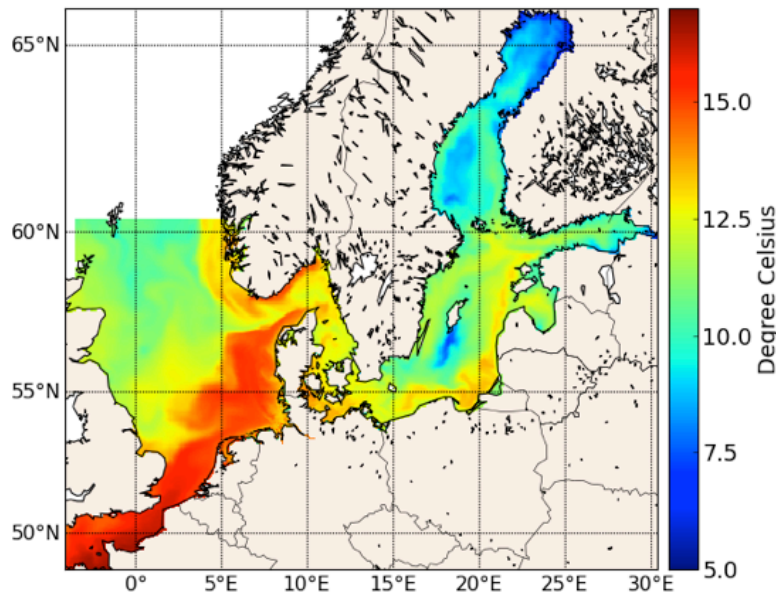
## Overview

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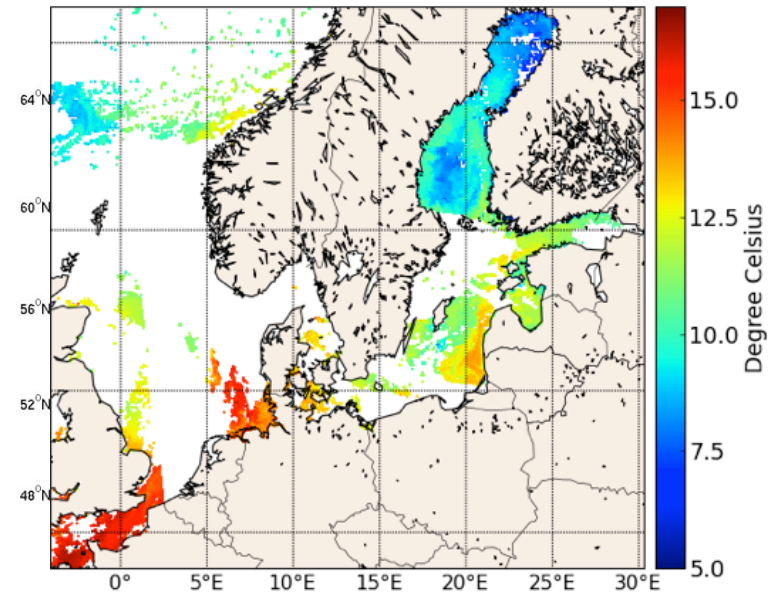
- Ensemble data assimilation
- Importance of software
- Coupled data assimilation
  - Challenges in two application examples

## Data assimilation

*Model surface temperature*



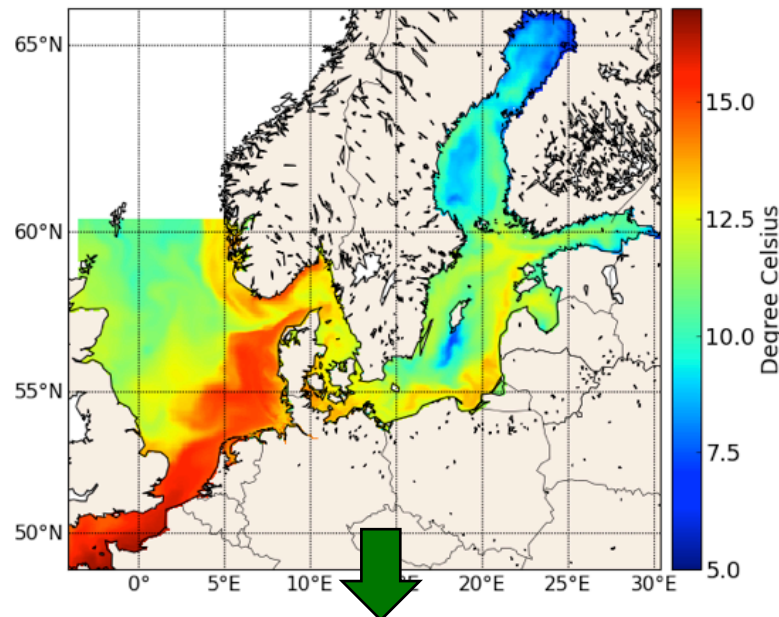
*Satellite surface temperature*



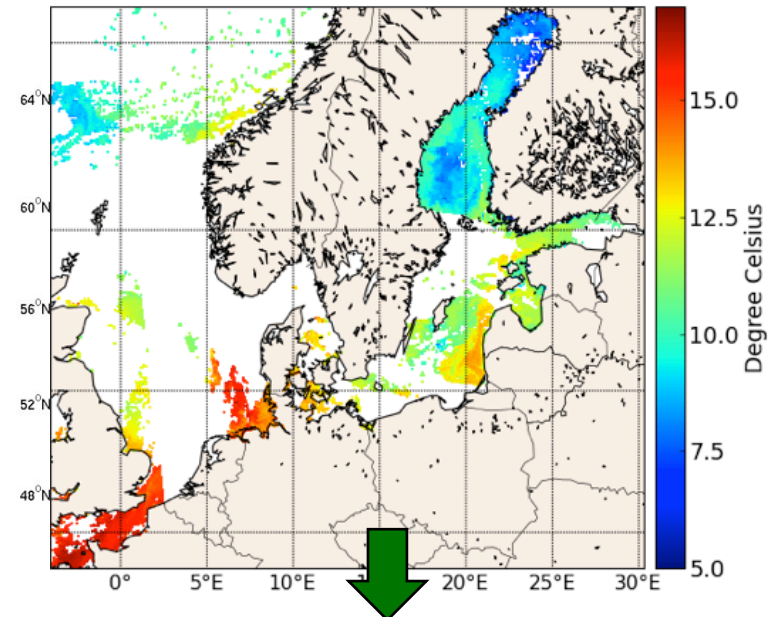
- Generally correct, but has errors
- all fields, fluxes on model grid
- Generally correct, but has errors
- incomplete information: data gaps, some fields
- ocean data: mainly surface (satellite)

# Data assimilation

*Model surface temperature*



*Satellite surface temperature*



Combine both sources of information  
quantitatively by computer algorithm  
→ Data Assimilation

# Data Assimilation

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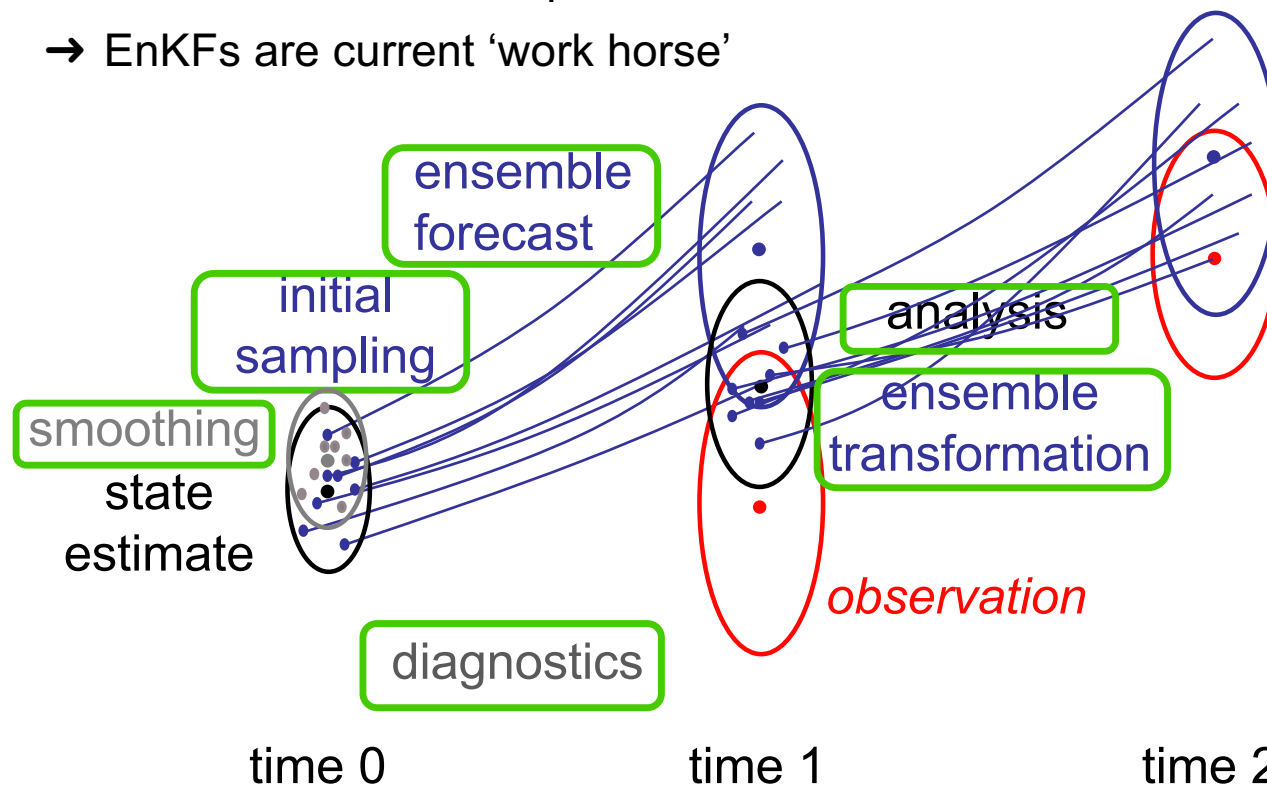
Methodology to combine model with real data

- Optimal estimation of system state:
  - initial conditions (for weather/ocean forecasts, ...)
  - state trajectory (temperature, concentrations, ...)
  - parameters (ice strength, plankton growth, ...)
  - fluxes (heat, primary production, ...)
  - boundary conditions and ‘forcing’ (wind stress, ...)
- More advanced: Improvement of model formulation
  - Detect systematic errors (bias)
  - Revise parameterizations based on parameter estimates

# Ensemble Data Assimilation

Ensemble Kalman Filters (EnKFs) & Particle Filters

- Use ensembles to represent probability distributions (uncertainty)
- Use observations to update ensemble
- EnKFs are current 'work horse'



There are many possible choices!

What is optimal is part of our research

Different choices in PDAF

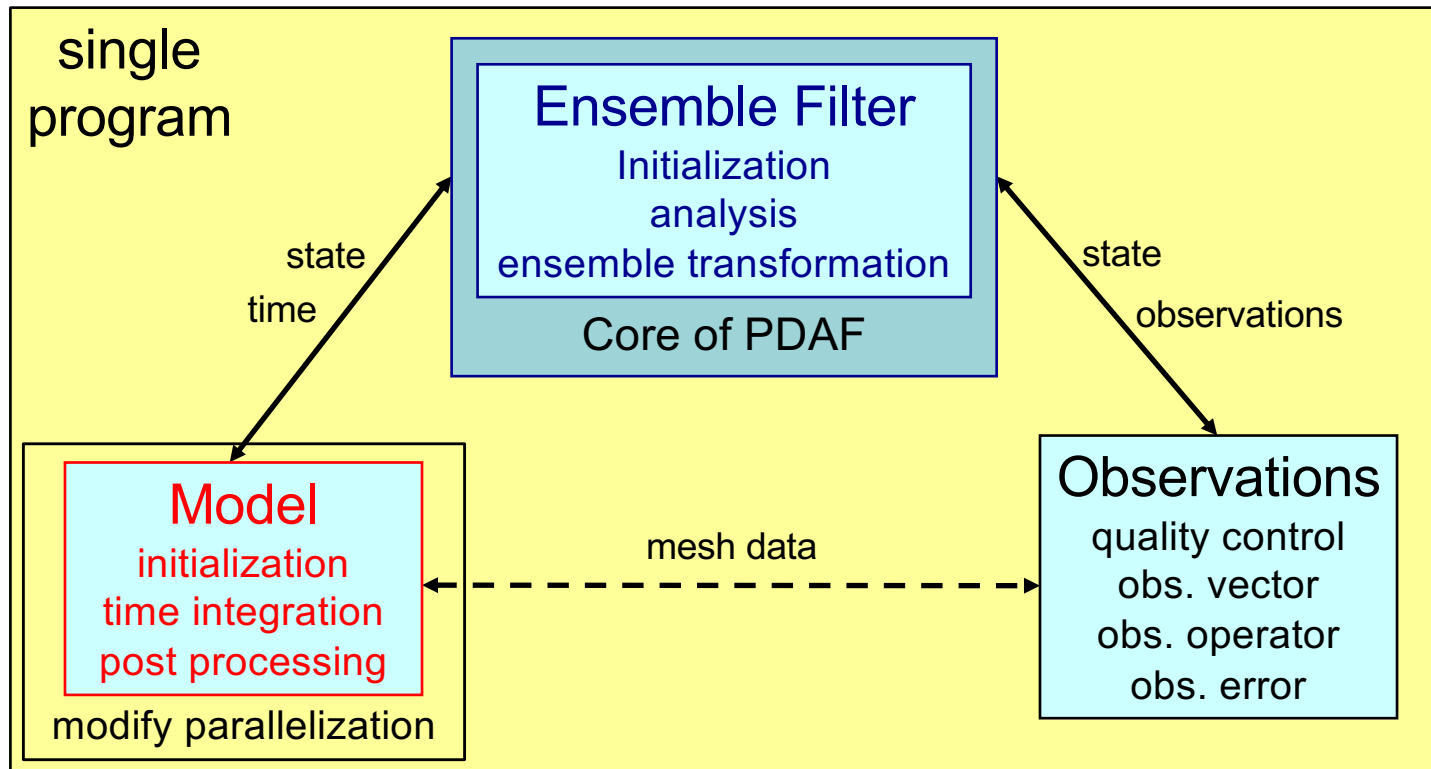
### PDAF - Parallel Data Assimilation Framework

- a program library for ensemble data assimilation
- provides support for parallel ensemble forecasts
- provides filters and smoothers - fully-implemented & parallelized (EnKF, LETKF, LESTKF, NETF, PF ... easy to add more)
- easily useable with (probably) any numerical model
- run from laptops to supercomputers (Fortran, MPI & OpenMP)
- Usable for real assimilation applications and to study assimilation methods
- first public release in 2004; continued development
- ~400 registered users; community contributions

Open source:  
Code, documentation, and tutorial available at

<http://pdaf.awi.de>

# 3 Components of Assimilation System

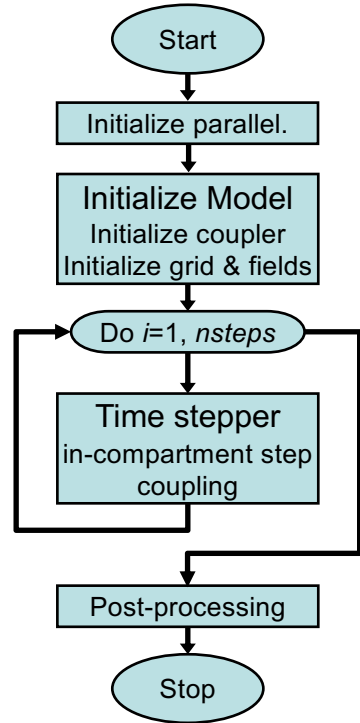


↔ Explicit interface  
- - - Indirect exchange (module/common)



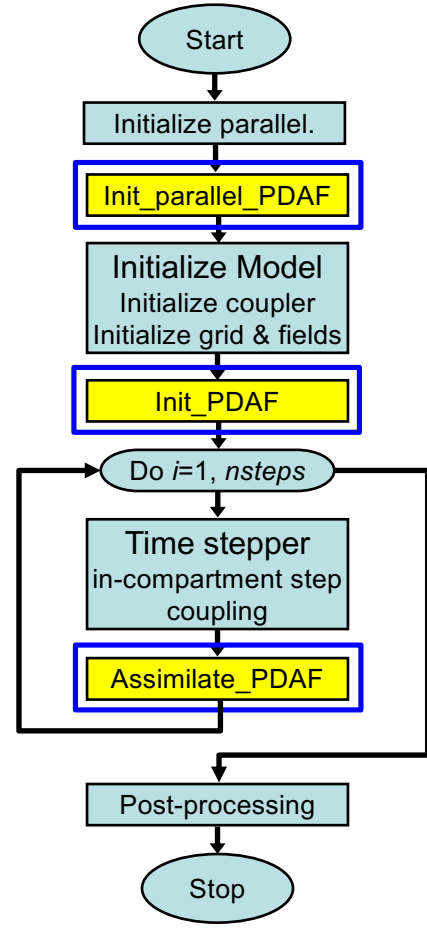
# Augmenting a Model for Data Assimilation

**Model**  
*single or multiple executables*  
*coupler might be separate program*



revised parallelization enables ensemble forecast

Extension for data assimilation

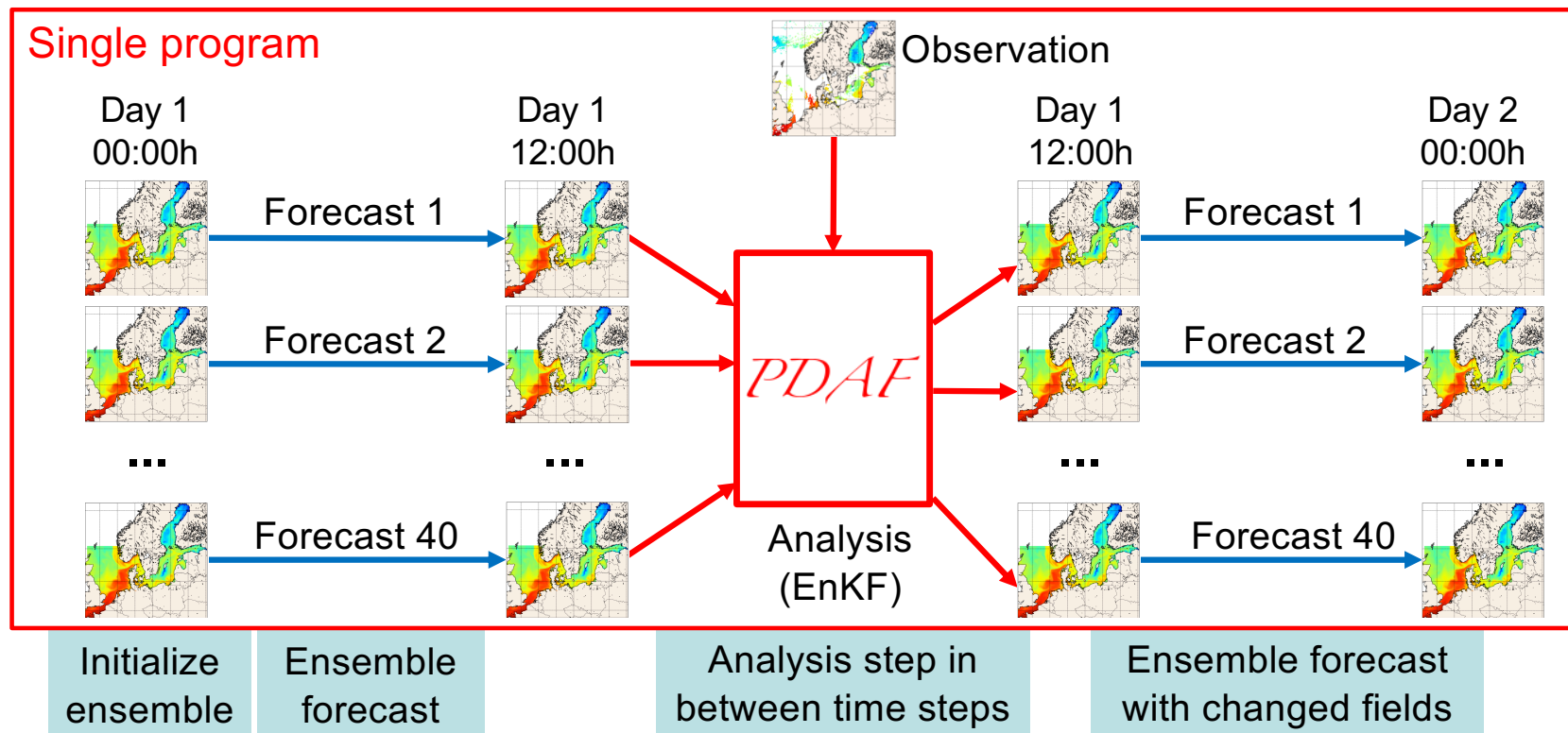


*plus:*  
 Possible model-specific adaption  
 e.g. in NEMO:  
 treat leap-frog time stepping

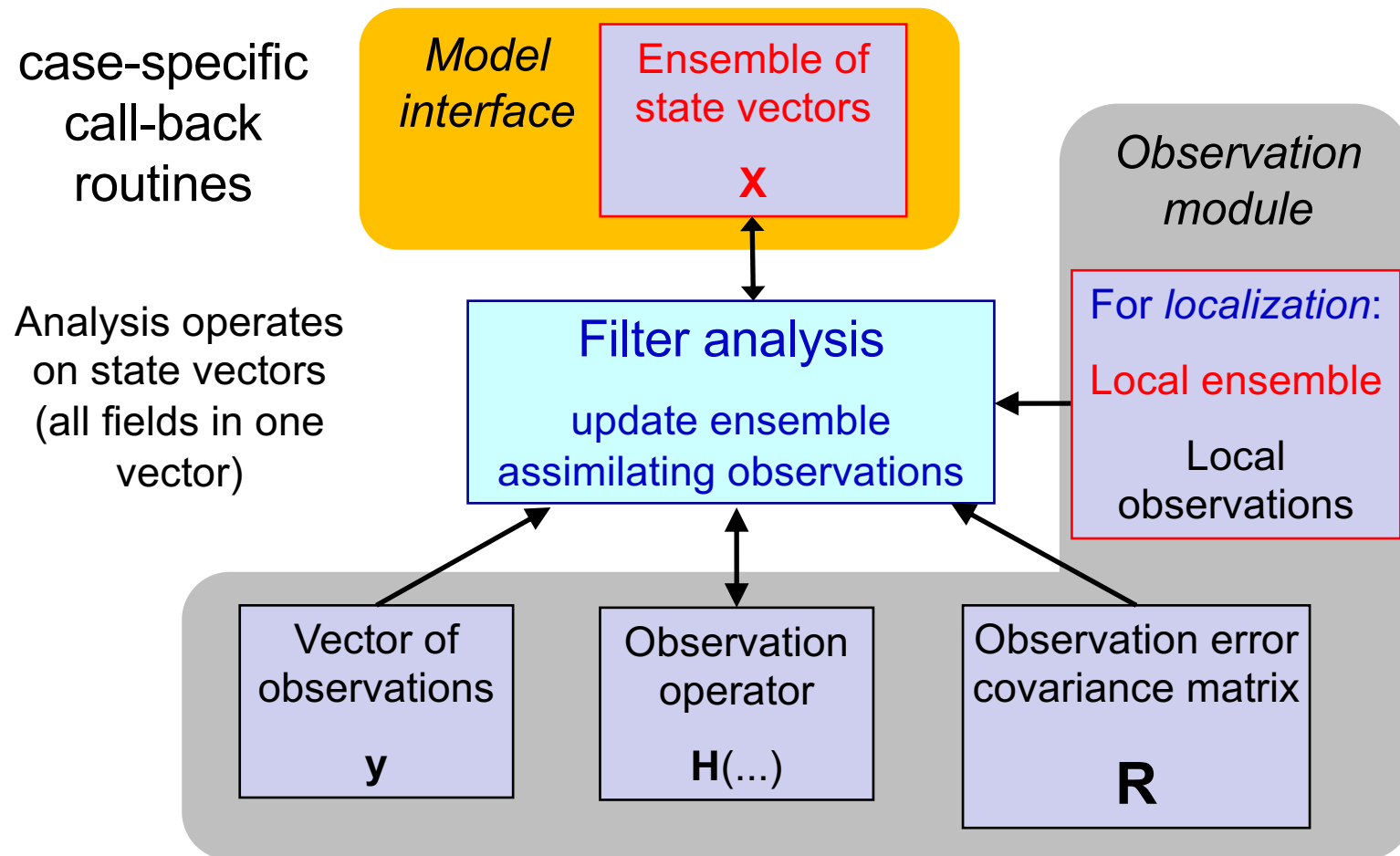
# Augmenting a Model for Data Assimilation

Couple PDAF with model

- Modify model to simulate ensemble of model states
- Insert correction step (analysis) to be executed at prescribed interval
- Run model as usual, but with more processors and additional options



# Ensemble Filter Analysis Step



## The Ensemble Kalman Filter (EnKF, Evensen 94)

Ensemble  $\{\mathbf{x}_0^{a(l)}, l = 1, \dots, N\}$

Ensemble covariance matrix  $\mathbf{P}_k^f := \frac{1}{N-1} \sum_{l=1}^N \left( \mathbf{x}_k^{f(l)} - \overline{\mathbf{x}_k^f} \right) \left( \mathbf{x}_k^{f(l)} - \overline{\mathbf{x}_k^f} \right)^T$

Ensemble mean (state estimate)  $\mathbf{x}_k^a := \frac{1}{N} \sum_{l=1}^N \mathbf{x}_k^{a(l)}$

### Analysis step:

Update each ensemble member

**Kalman filter**

$$\mathbf{x}_k^{a(l)} = \mathbf{x}_k^{f(l)} + \mathbf{K}_k \left( \mathbf{y}_k^{(l)} - \mathbf{H}_k \mathbf{x}_k^{f(l)} \right)$$

$$\mathbf{K}_k = \mathbf{P}_k^f \mathbf{H}_k^T \left( \mathbf{H}_k \mathbf{P}_k^f \mathbf{H}_k^T + \mathbf{R}_k \right)^{-1}$$

**Expensive to compute**

If elements of  $\mathbf{x}$  are observed:

- $\mathbf{K}$  contains
  - observed rows
  - unobserved rows

Unobserved variables updated through cross-covariances in  $\mathbf{P}$  (linear regression)

# Current algorithms in PDAF

PDAF originated from comparison studies of different filters

## Filters and smoothers

- EnKF (Evensen, 1994 + perturbed obs.)
- (L)ETKF (Bishop et al., 2001)
- SEIK filter (Pham et al., 1998)
- **ESTKF** (Nerger et al., 2012)
- NETF (Toedter & Ahrens, 2015)
- Particle filter (PF)
- Generate synthetic observations

Not yet released:

- serial EnSRF
- EWPF

## All methods include (except PF)

- global and localized versions
- smoothers

## Model binding

- MITgcm

## Toy models

- Lorenz-96, Lorenz63

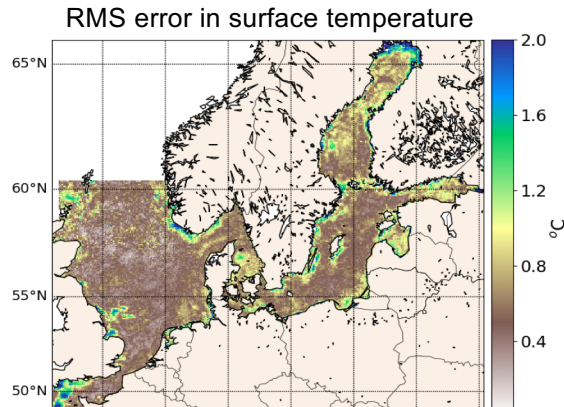
Not yet released:

- AWI-CM model binding
- NEMO model binding

# PDAF Application Examples

## HBM-ERGOM:

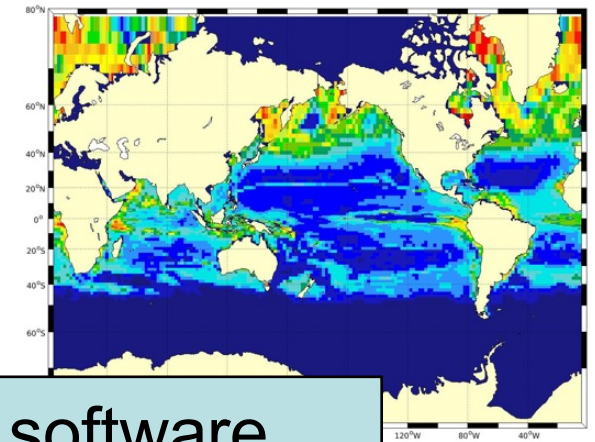
Coastal  
assimilation of  
SST, in situ and  
ocean color data  
(Svetlana Losa,  
Michael Goodliff)



## MITgcm-REcoM:

global ocean color  
assimilation  
(Himansu Pradhan)

Total chlorophyll concentration June 30, 2012

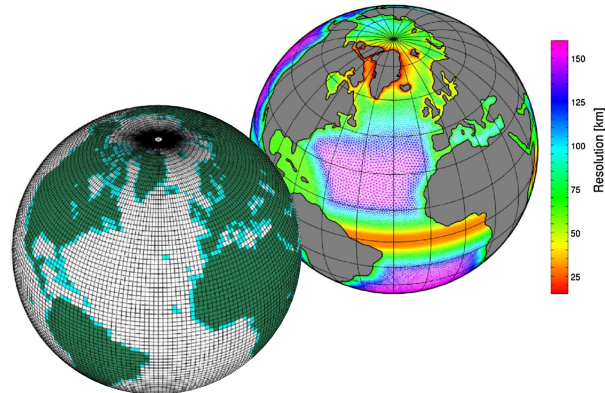


Different models – same assimilation software

## AWI-CM:

coupled  
atmos.-ocean  
assimilation  
(Qi Tang,  
Longjiang Mu)

AWI-CM: ECHAM6-FESOM coupled model



+ external applications & users, like

- MITgcm sea-ice assim (NMEFC Beijing)
- Geodynamo (IPGP Paris, A. Fournier)
- TerrSysMP-PDAF (hydrology, FZ Juelich)
- CMEMS Baltic-MFC (operational, DMI/BSH/SMHI)
- CFSv2 (J. Liu, IAP-CAS Beijing)
- NEMO (U. Reading , P. J. van Leeuwen)

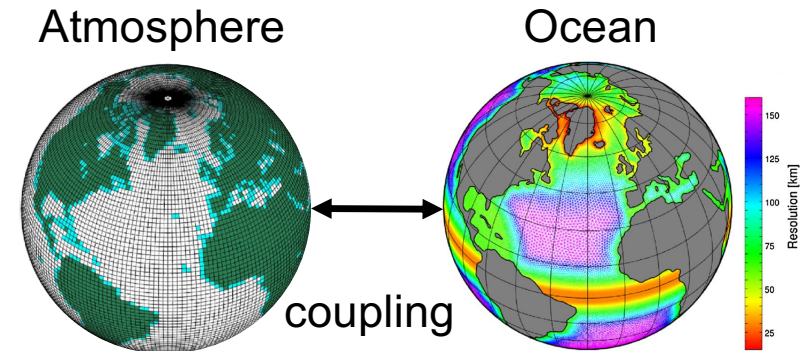
# Coupled Models and Coupled Data Assimilation

## Coupled models

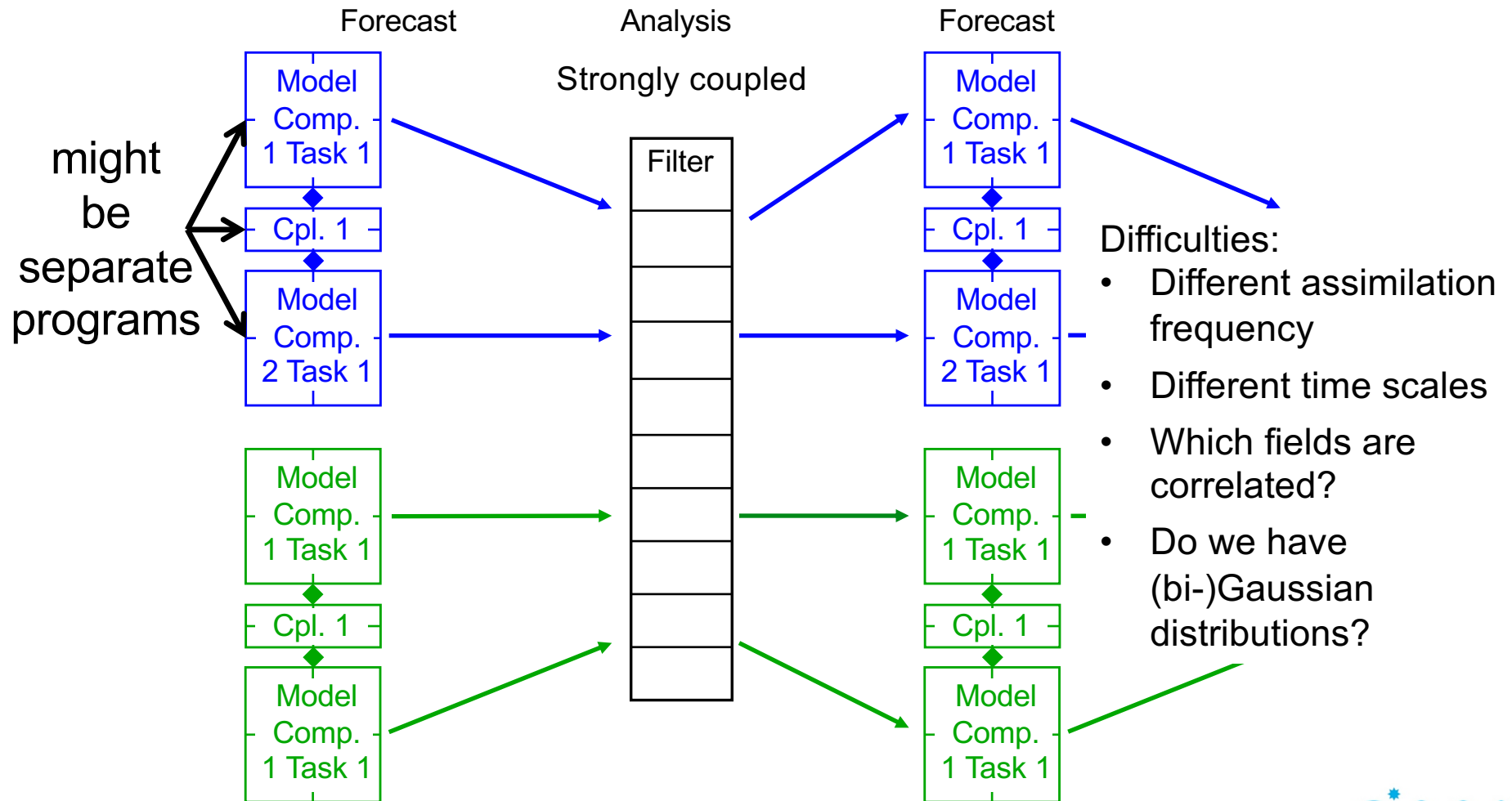
- Several interconnected compartments, like
  - Atmosphere and ocean
  - Ocean physics and biogeochemistry (carbon, plankton, etc.)

## Coupled data assimilation

- Assimilation into coupled models
  - Weakly coupled: separate assimilation in the compartments
  - Strongly coupled: joint assimilation of the compartments
    - Use cross-covariances between fields in compartments
- Plus various “in between” possibilities ...

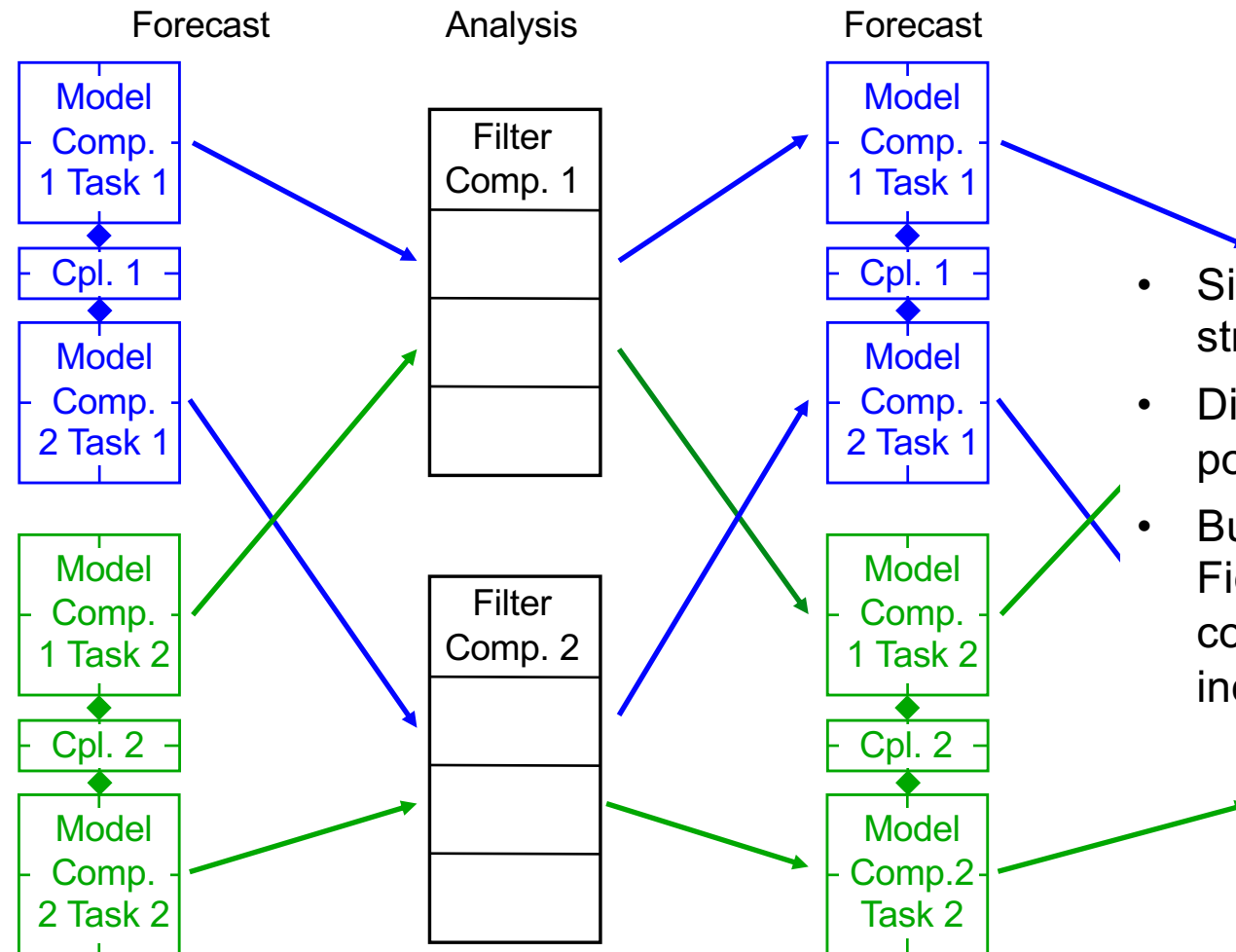


## 2 compartment system – strongly coupled DA





## 2 compartment system – weakly coupled DA



- Simpler setup than strongly coupled
- Different DA methods possible
- But:  
Fields in different compartments can be inconsistent

# Example 1

## Assimilation into the coupled atmosphere-ocean model AWI-CM

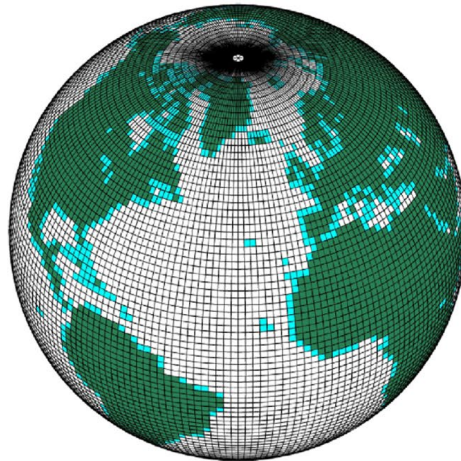
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(Qi Tang)

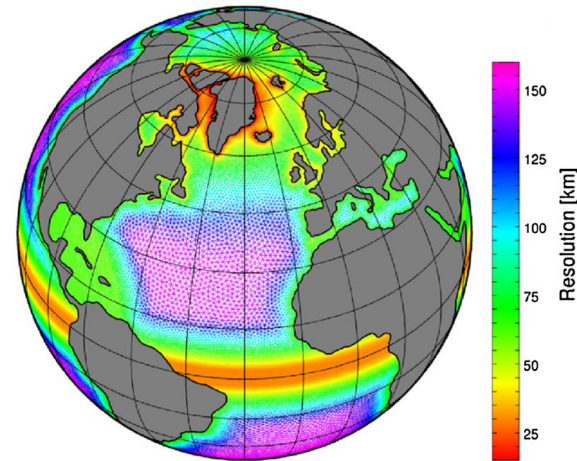
Project: ESM – Advanced Earth System Modeling Capacity

# Assimilation into coupled model: AWI-CM

Atmosphere



Ocean



OASIS3-MCT  
fluxes  
ocean/ice state

**Atmosphere**

- ECHAM6
- JSBACH land

**Coupler library**

- OASIS3-MCT

**Ocean**

- FESOM
- includes sea ice

Two separate executables for atmosphere and ocean

**Goal: Develop data assimilation methodology for cross-domain assimilation (“strongly-coupled”)**

# Data Assimilation Experiments

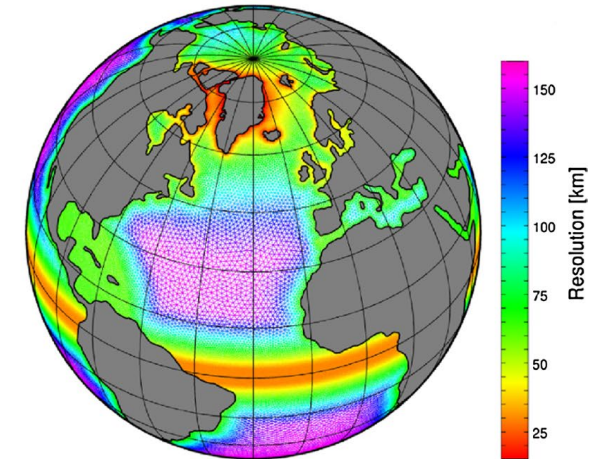
## Model setup

- Global model
- ECHAM6: T63L47
- FESOM: resolution 30-160km

## Data assimilation experiments

- Observations
  - Satellite SST
  - Profiles temperature & salinity
- Updated: ocean state (SSH, T, S, u, v, w)
- Assimilation method: Ensemble Kalman Filter (LESTKF)
- Ensemble size: 46
- Simulation period: year 2016, daily assimilation update
- Run time: 5.5h, fully parallelized using 12,000 processor cores

FESOM mesh resolution



## Offline coupling - Efficiency

Offline-coupling is simple to implement  
but can be very inefficient

### Example:

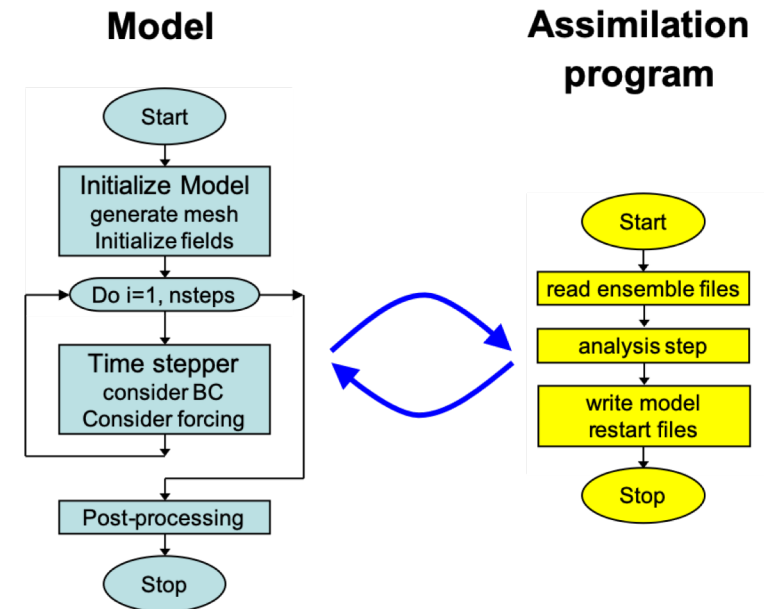
Timing from atmosphere-ocean  
coupled model (AWI-CM)  
with daily analysis step:

Model startup:	95 s	} overhead
Integrate 1 day:	28 s	
Model postprocessing:	14 s	

Analysis step:	1 s
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Restarting this model is ~3.5 times  
more expensive than integrating 1 day

→ avoid this for data assimilation



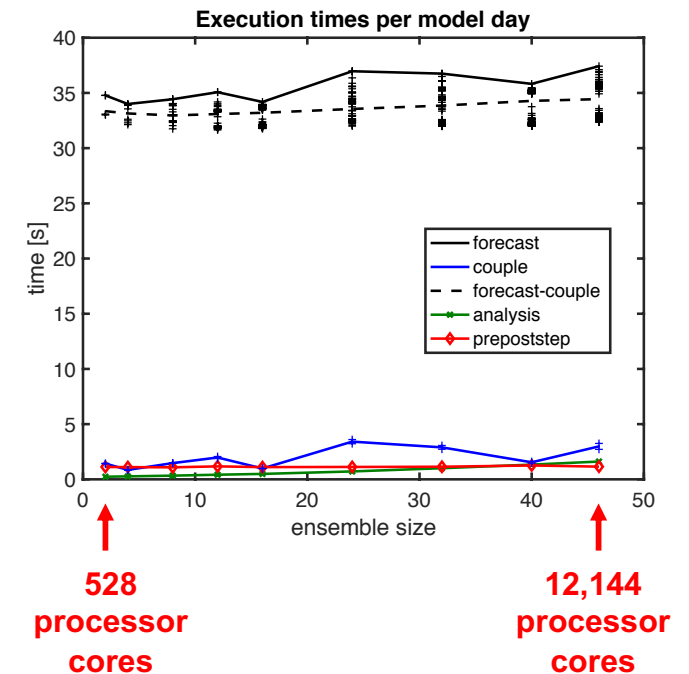
## Execution times (weakly-coupled, DA only into ocean)

### MPI-tasks

- ECHAM: 72
- FESOM: 192
- Increasing integration time with growing ensemble size (11%; more parallel communication; worse placement)
- some variability in integration time over ensemble tasks

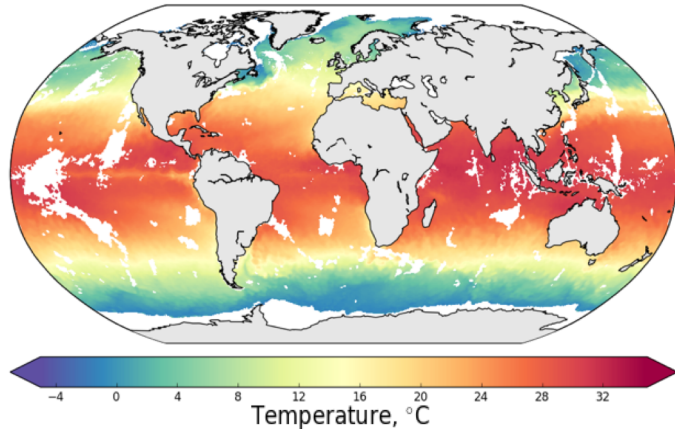
### Important factors for good performance

- Need optimal distribution of programs over compute nodes/racks (here set up as ocean/atmosphere pairs)
- Avoid conflicts in IO (Best performance when each AWI-CM task runs in separate directory)



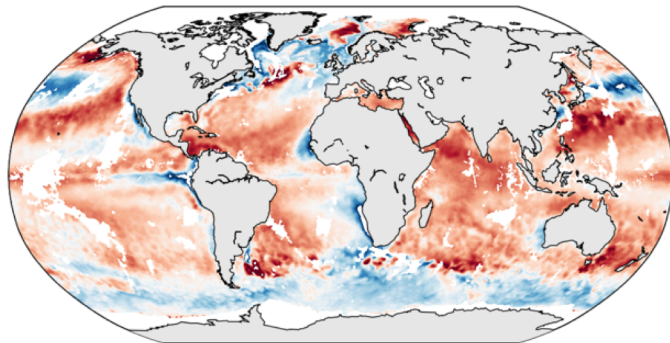
# Assimilate sea surface temperature (SST)

SST on Jan 1<sup>st</sup>, 2016



- Satellite sea surface temperature (level 3, EU Copernicus)
- Daily data
- Data gaps due to clouds
- Observation error: 0.8 °C
- Localization radius: 1000 km

SST difference: observations-model



Large initial SST deviation due to using a coupled model: up to 10°C



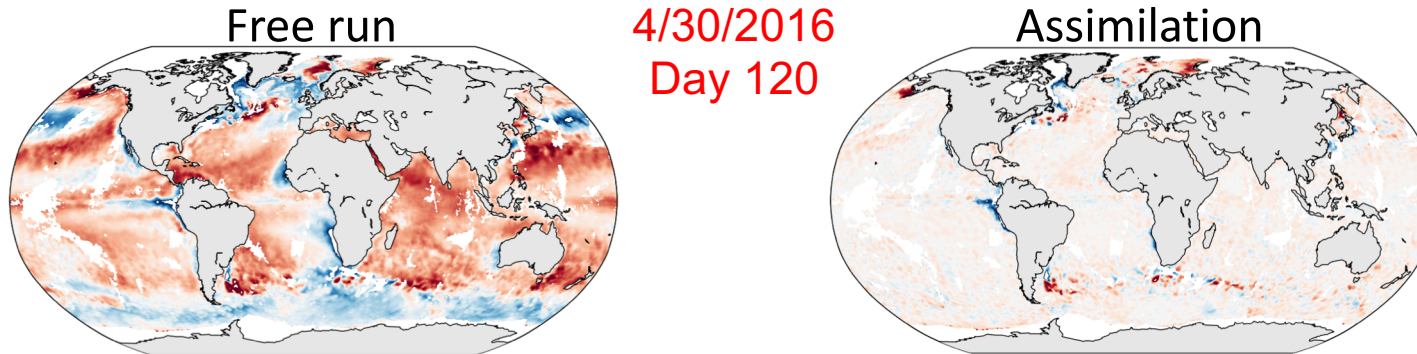
DA with such a coupled model is unstable!



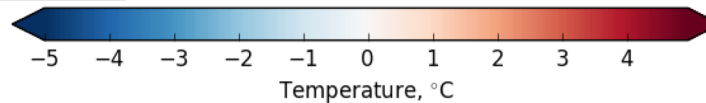
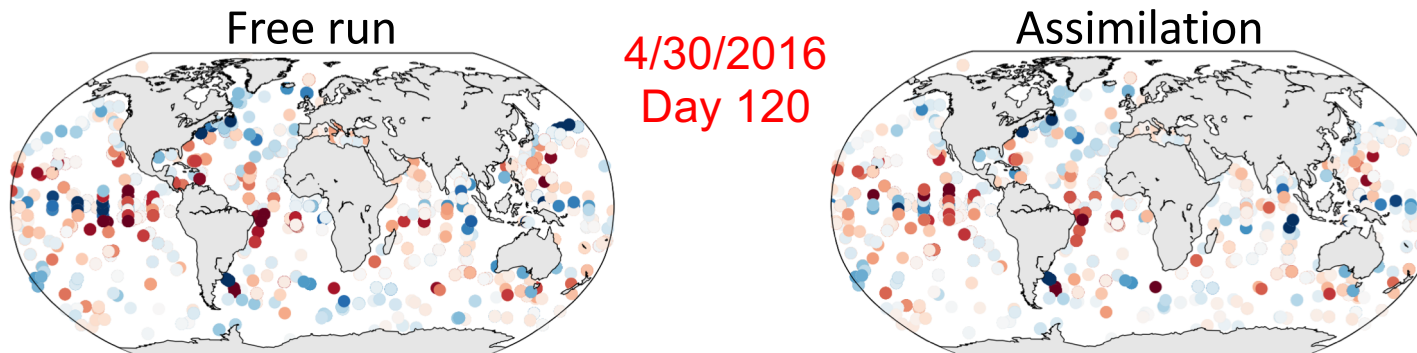
omit SST observations where  
 $|SST_{obs} - SST_{ens\_mean}| > 1.6 \text{ °C}$   
(30% initially, <5% later)

## SST assimilation: Effect on the ocean

SST difference (obs-model): strong decrease of deviation



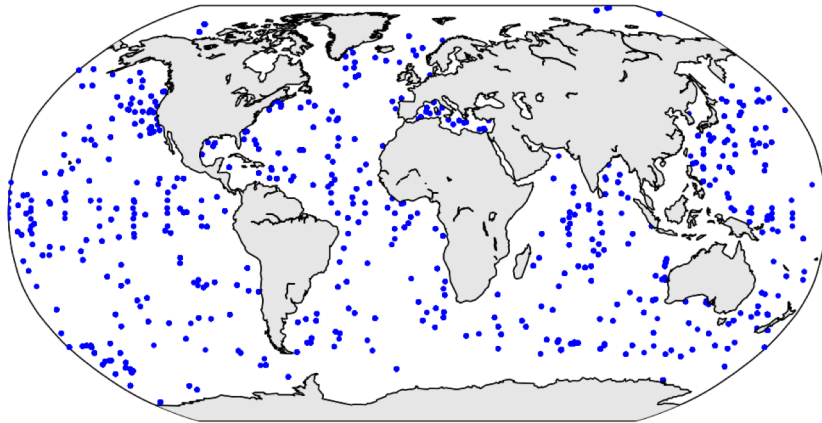
Subsurface temperature difference (obs-model); all the model layers at profile locations





## Assimilate subsurface observations: Profiles

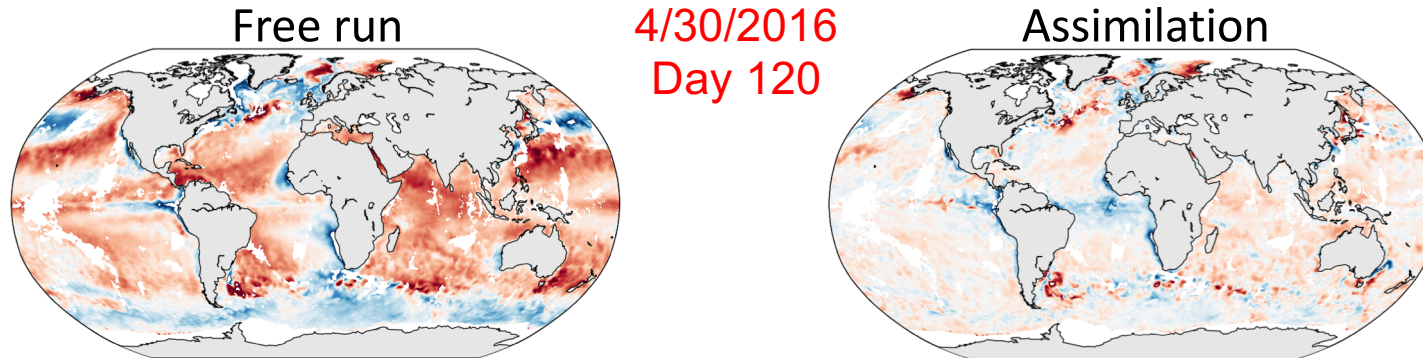
Profile locations on Jan 1<sup>st</sup>, 2016



- Temperature and Salinity
- EN4 data from UK MetOffice
- Daily data
- Subsurface down to 5000m
- About 1000 profiles per day
- Observation errors
  - Temperature profiles: 0.8 °C
  - Salinity profiles: 0.5 psu
- Localization radius: 1000 km

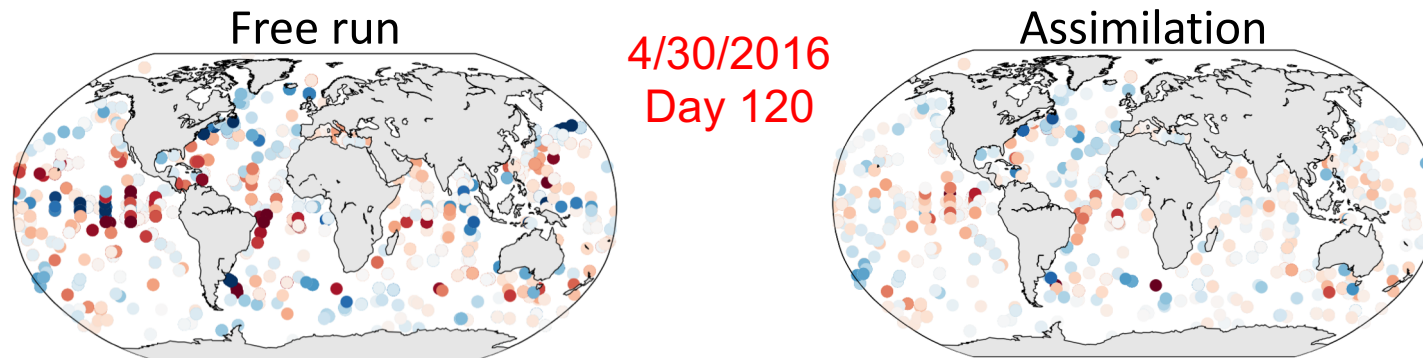
# SST assimilation: Effect on the ocean

SST difference (obs-model)

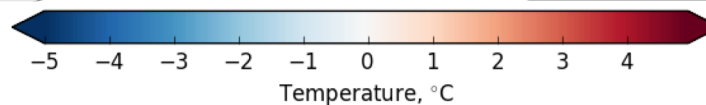


larger deviations  
than for SST  
assimilation

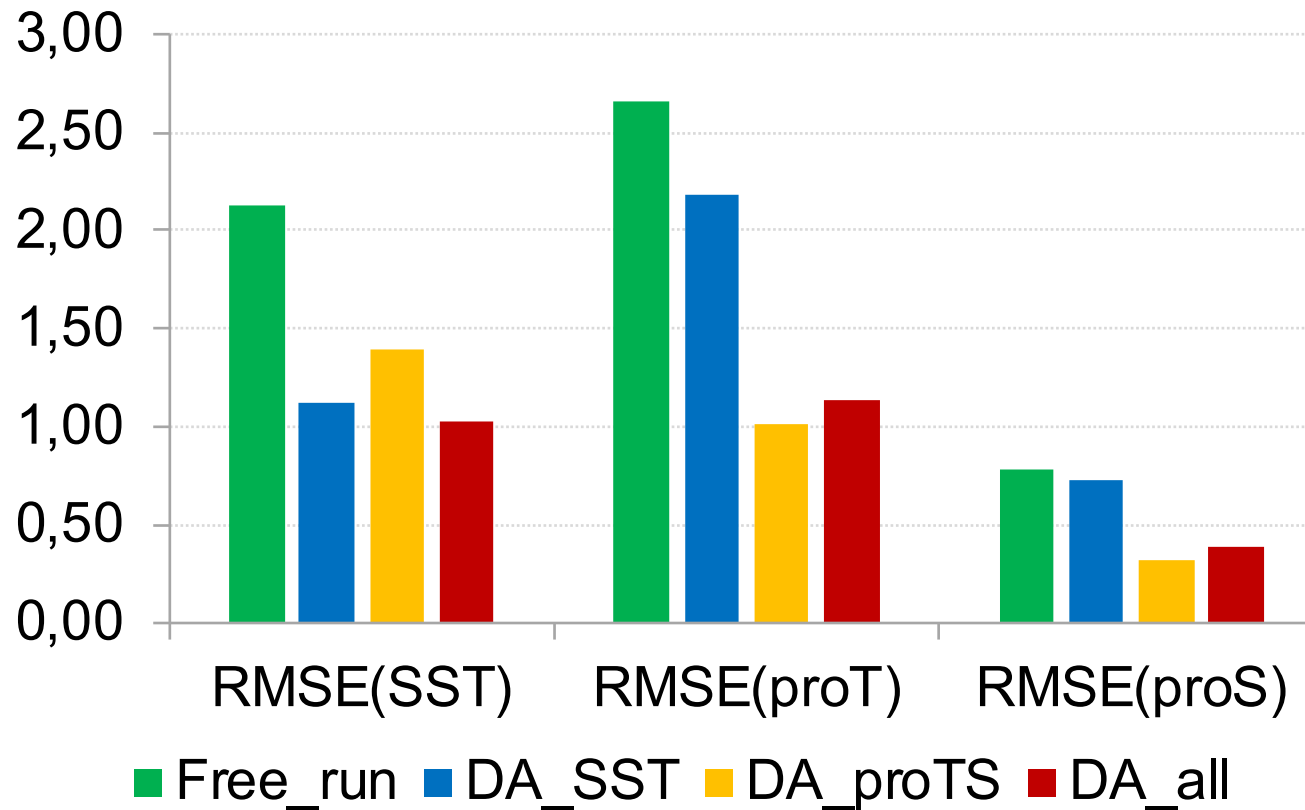
Subsurface temperature difference (obs-model); all the model layers at profile locations



smaller deviations  
than for SST  
assimilation



## Assimilation effect: RMS errors



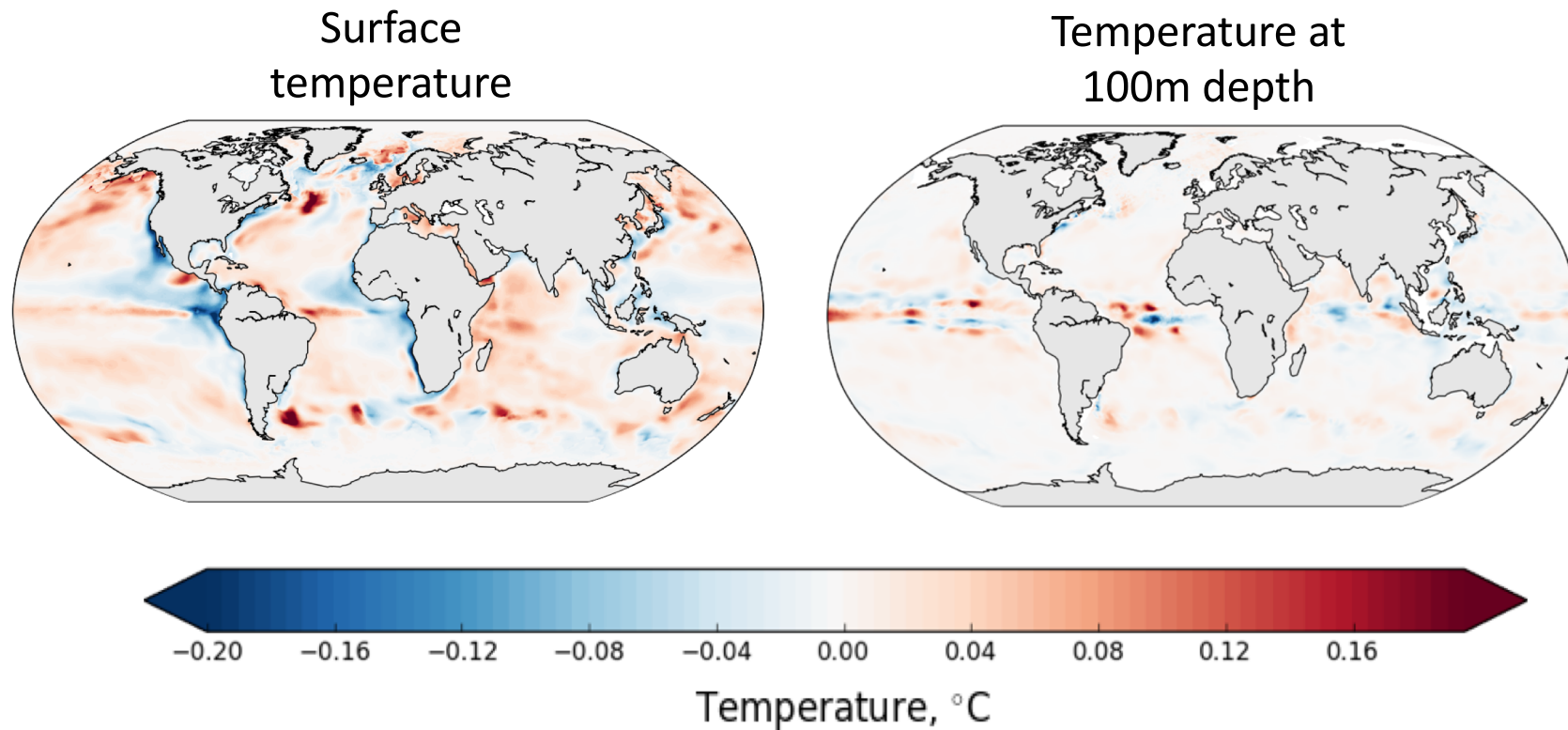
Overall lowest errors with combined assimilation

- But partly a compromise

## Mean increments

Mean increments (analysis – forecast) for days 61-366 (after spinup)

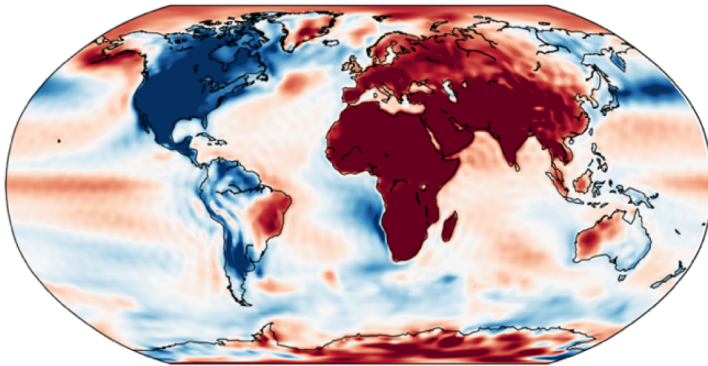
→ non-zero values indicate regions with possible biases



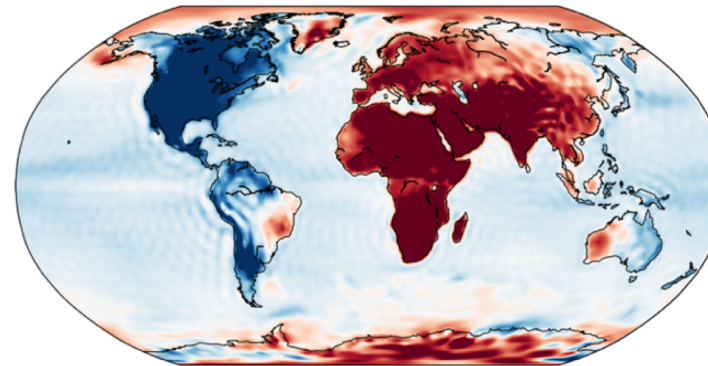
# Effect on Atmospheric State (annual mean)

2-meter temperature

Free run



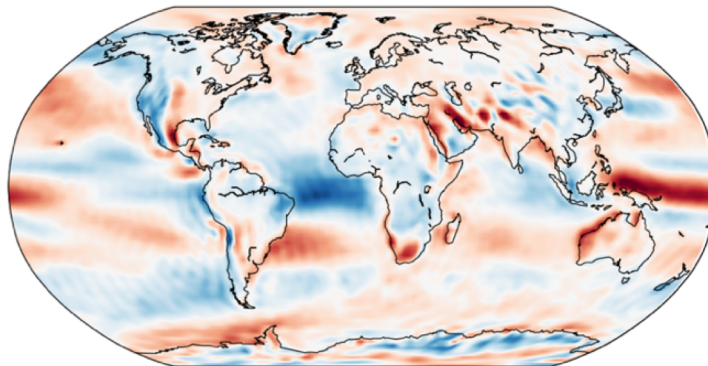
Assimilation



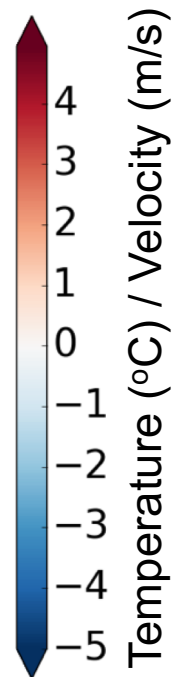
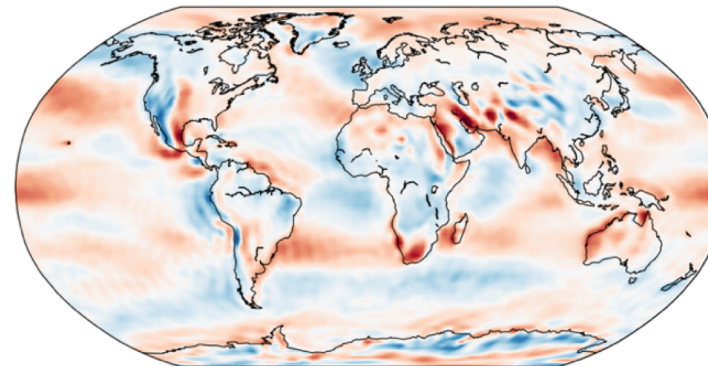
Relevant is ocean surface

10 meter zonal wind velocity

Free run



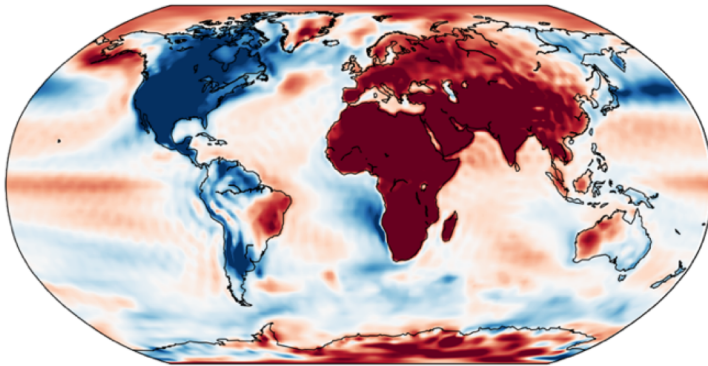
Assimilation



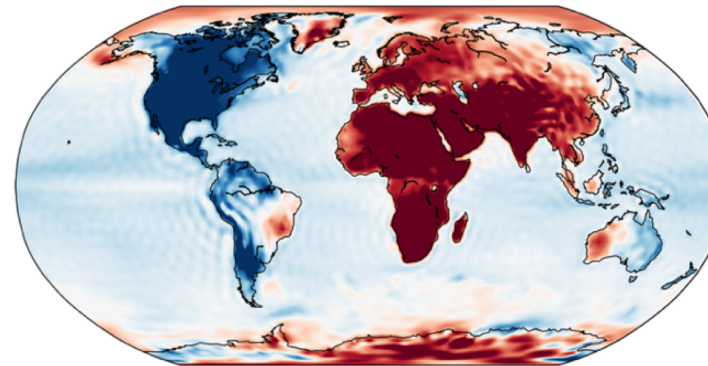
## Effect on Atmospheric State (annual mean)

2-meter temperature

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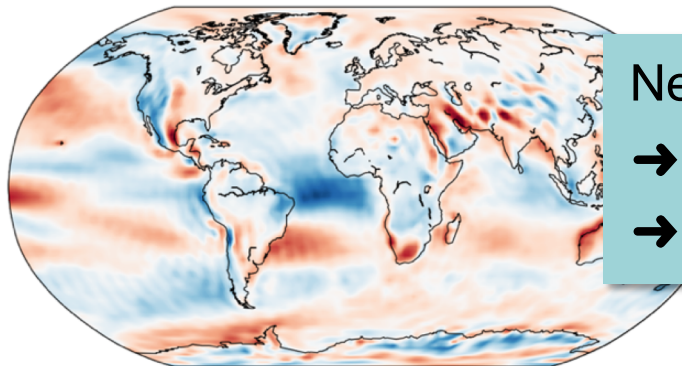
Assimilation



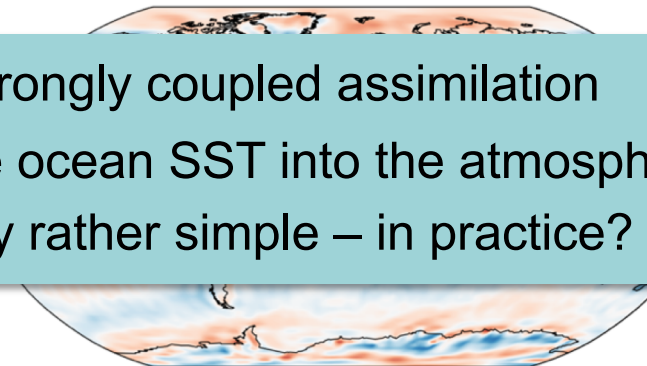
Relevant is ocean surface

10 meter zonal wind velocity

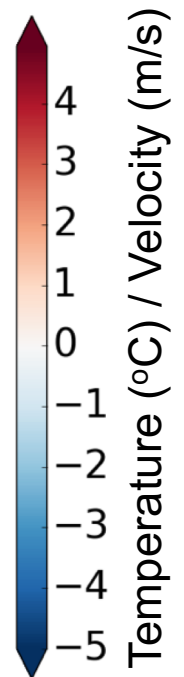
Free run



Assimilation



Next step: strongly coupled assimilation  
→ assimilate ocean SST into the atmosphere  
→ technically rather simple – in practice?



## Example 2

# Weakly- and Strongly Coupled Assimilation to Constrain Biogeochemistry with Temperature Data

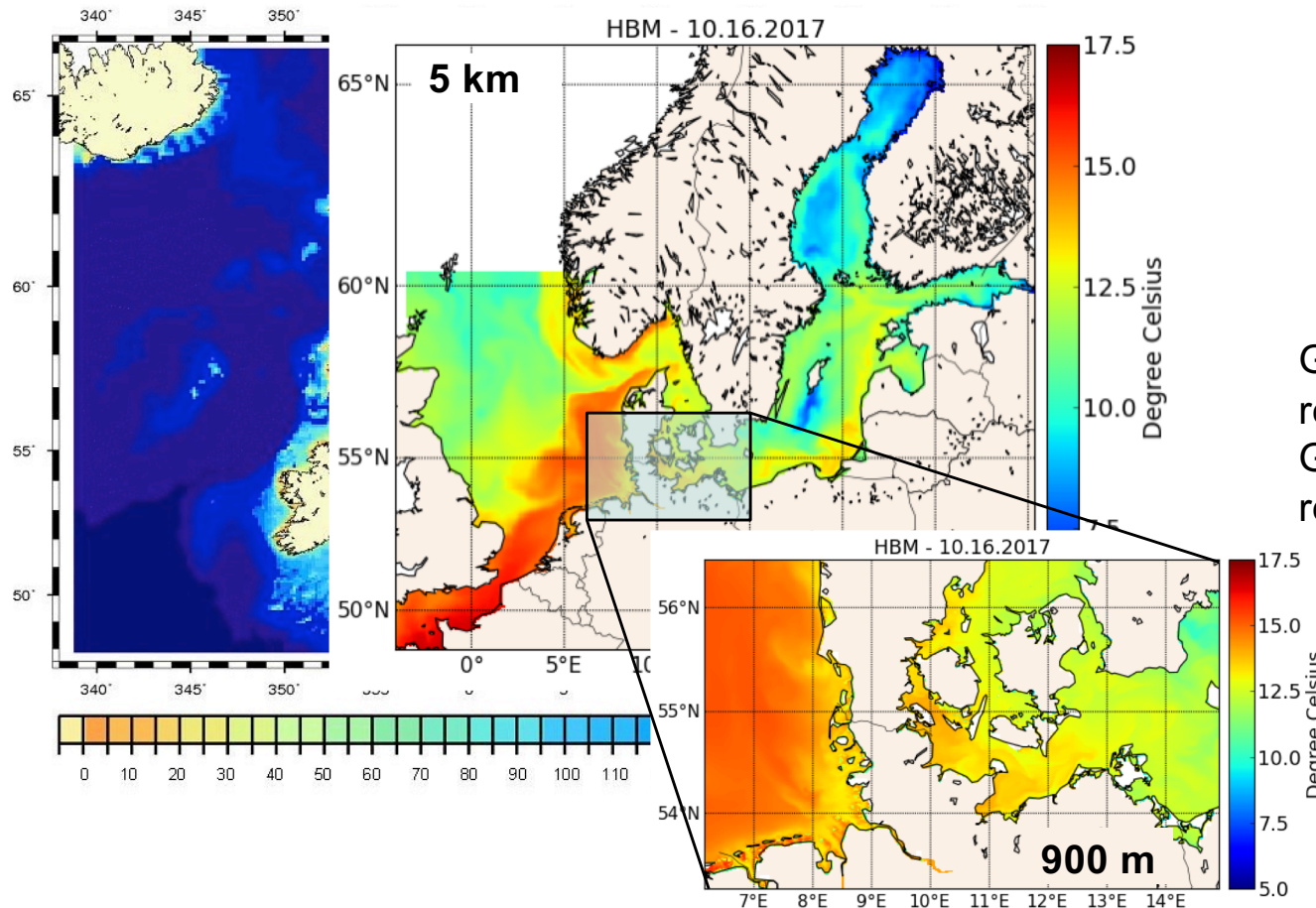
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(MERAMO – Mike Goodliff)

Cooperation with German Hydrographic Agency (BSH)  
(Ina Lorkowski, Xin Li, Anja Lindenthal, Thoger Brüning)

# Coastal Model Domain

**HBM (Hiromb-BOOS Model) – operationally used at German Federal Maritime and Hydrographic Agency (BSH)**

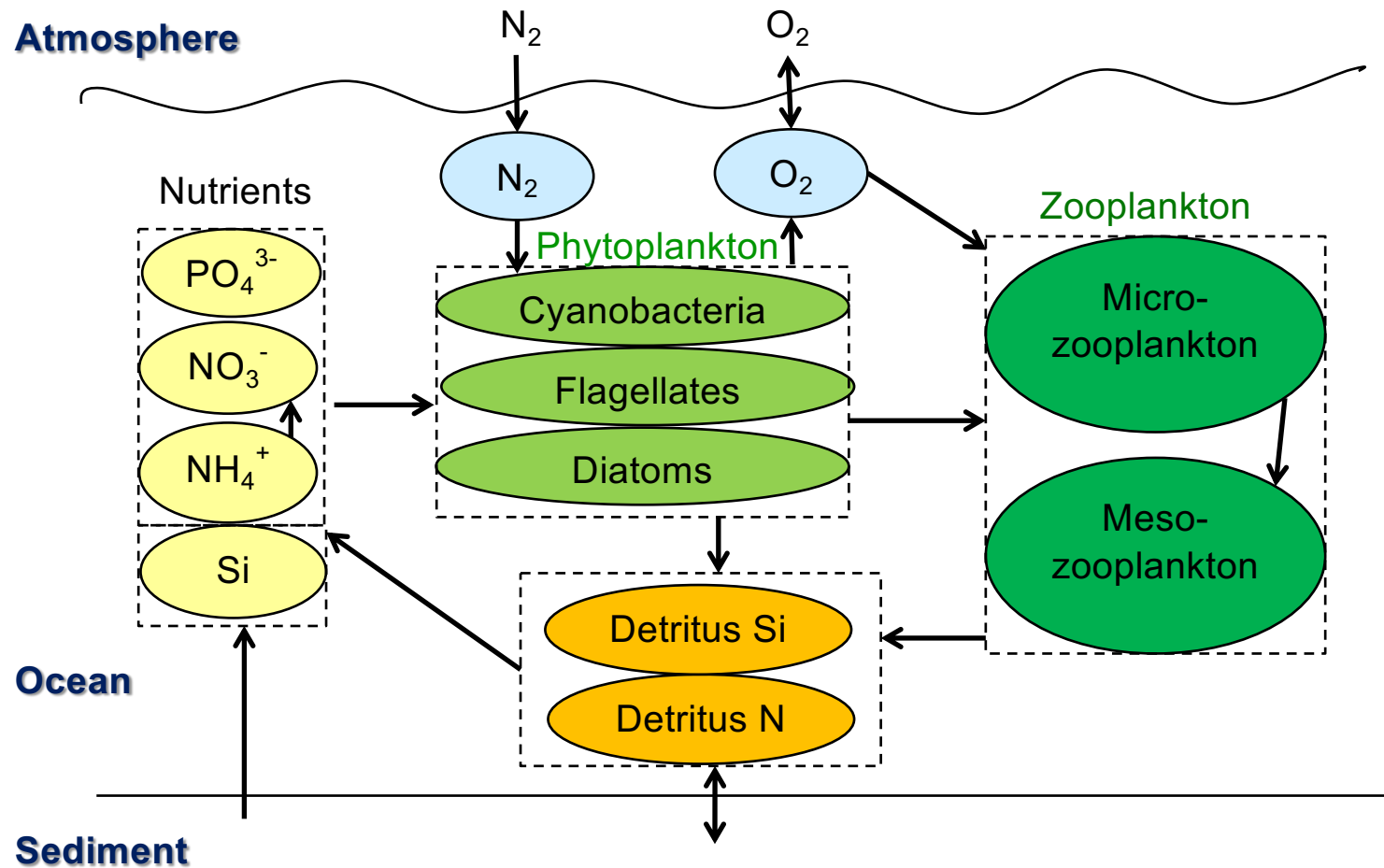


Grid with higher resolution in German coastal region

Lars Nerger et al. – Ensemble DA with PDAF



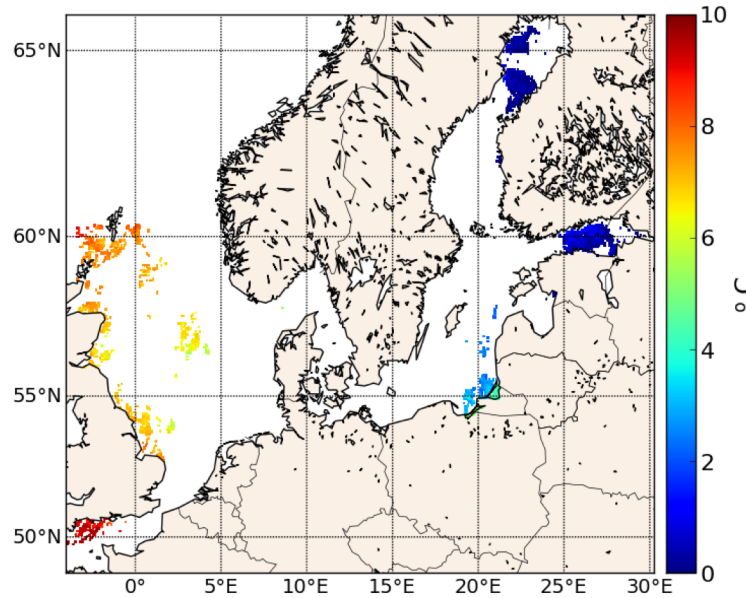
# Biogeochemical model: ERGOM



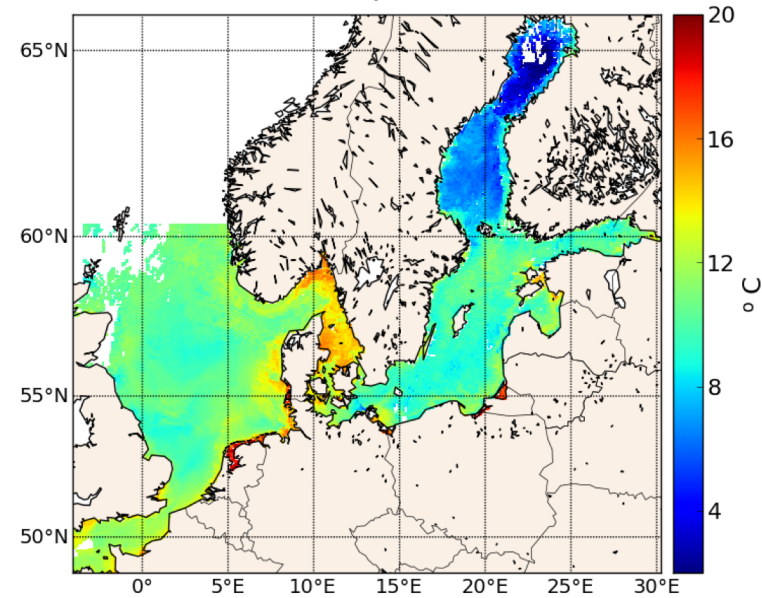
## Observations – Sea Surface Temperature (SST)

NOAA/AVHRR Satellite data

10 April 2012



25 May 2012



- 12-hour composites on both model grids
- Vastly varying data coverage (due to clouds)
- Effect on biogeochemistry?

## Comparison with assimilated SST data (4-12/2012)

- RMS deviation from SST observations up to  $\sim 0.4$  °C

### Coarse grid:

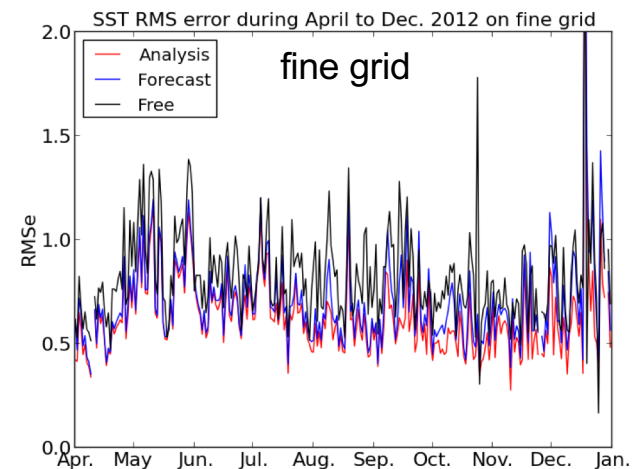
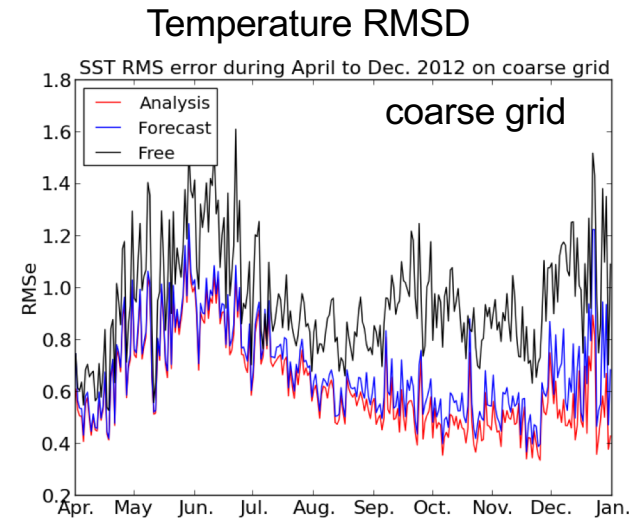
- Increasing error-reductions compared to free ensemble run

### Fine grid:

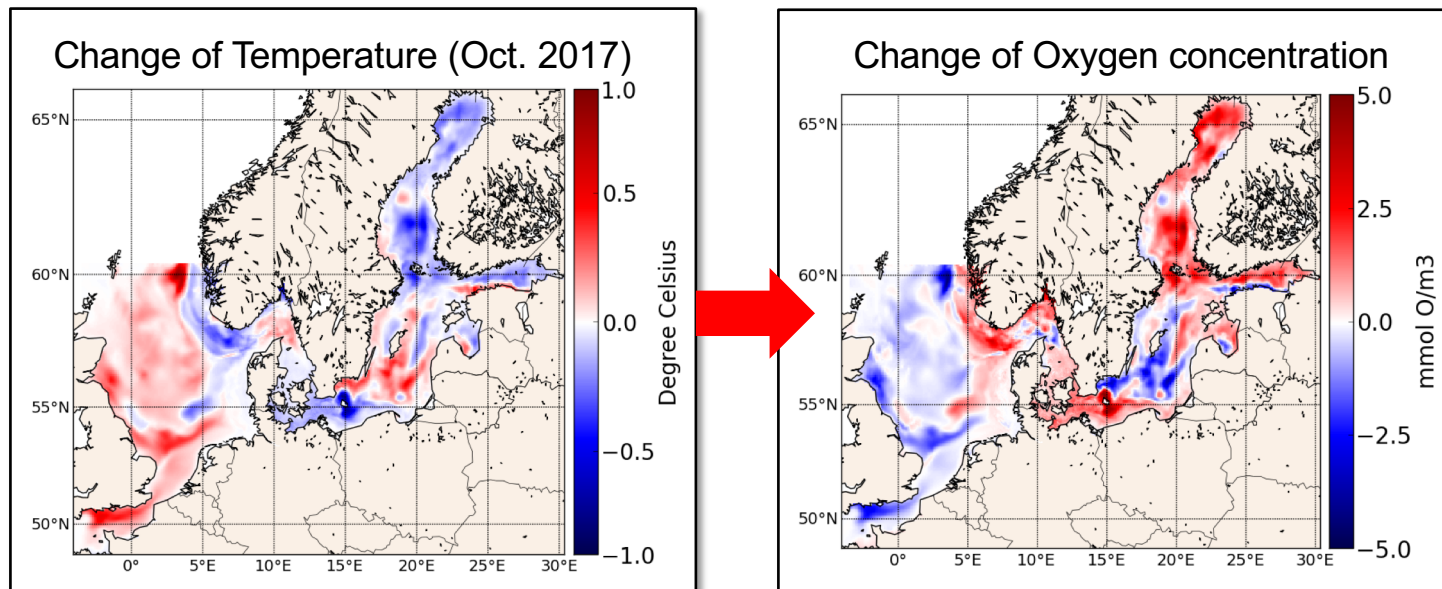
- much stronger variability
- Forecast errors sometimes reach errors of free ensemble run

### RMS errors (deg. C)

	Free	Forec.	Ana.
Coarse	0.95	0.68	0.63
Fine	0.83	0.70	0.63



## Influence of Assimilation on Surface Temperature

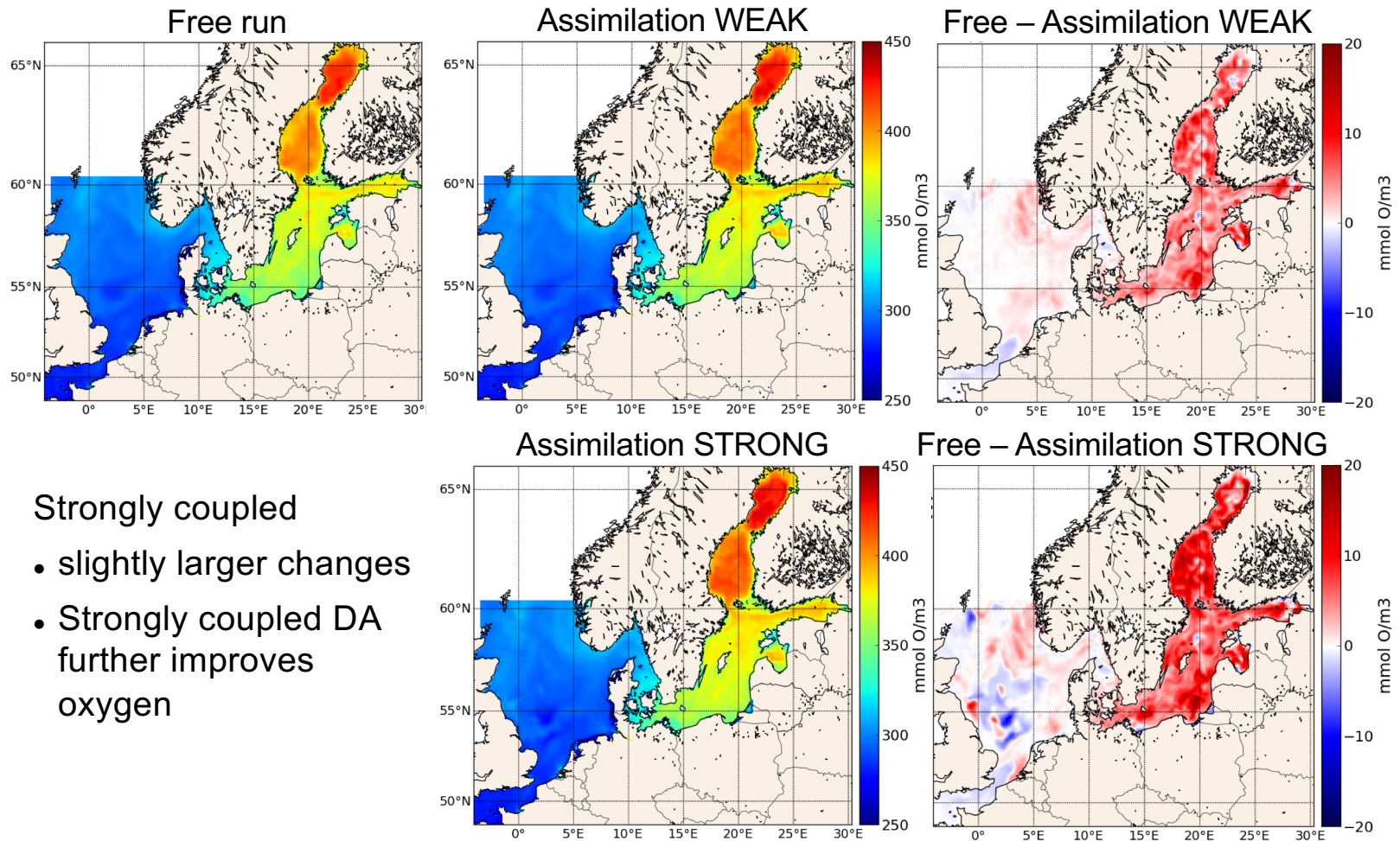


2 ways of influence:

- Indirect - *weakly-coupled assimilation*  
model dynamics react on change in physics
- Direct – *strongly-coupled assimilation*  
use cross-covariances between surface temperature and biogeochemistry

# Weakly & strongly coupled effect on biogeochemical model

Oxygen mean for May 2012 (as mmol O / m<sup>3</sup>)



Strongly coupled

- slightly larger changes
- Strongly coupled DA further improves oxygen

## Choice of variable in strongly coupled assimilation

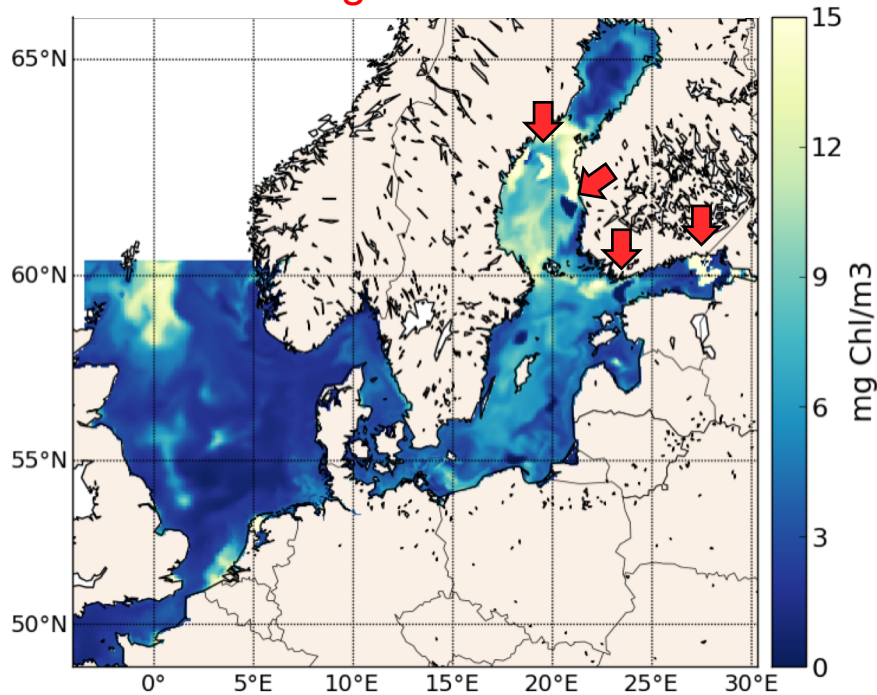
- Chlorophyll is lognormally distributed
  - Ensemble Kalman filter
    - Optimality for normal distributions
    - Linear regression between observed and unobserved variables
- Apply strongly-coupled DA with logarithm on concentrations?

**Kalman filter**

$$\mathbf{x}_k^{a(l)} = \mathbf{x}_k^{f(l)} + \mathbf{K}_k \left( \mathbf{y}_k^{(l)} - \mathbf{H}_k \mathbf{x}_k^{f(l)} \right)$$
$$\mathbf{K}_k = \mathbf{P}_k^f \mathbf{H}_k^T \left( \mathbf{H}_k \mathbf{P}_k^f \mathbf{H}_k^T + \mathbf{R}_k \right)^{-1}$$
$$\mathbf{K}_k = \underbrace{\mathbf{X}'_k}_{\text{model}} \underbrace{\left( \mathbf{H}_k \mathbf{X}'_k \right)^T \left( \mathbf{H}_k \mathbf{P}_k^f \mathbf{H}_k^T + \mathbf{R}_k \right)^{-1}}_{\text{observations}}$$

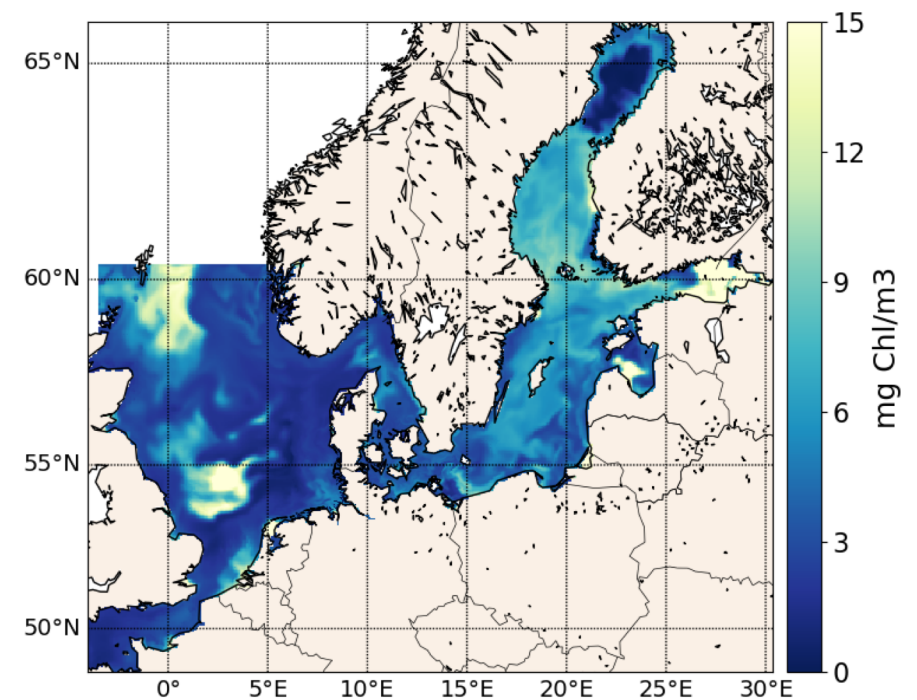
## Choice of variable in strongly coupled assimilation

Strongly coupled  
logarithmic



- locally unrealistically high and low concentrations  
→ Linear regression with lognormal concentration not general solution

Strongly coupled  
linear



- Larger effect – in particular in North Sea
- Too high in Gulf of Finland

## Summary

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- Coupled data assimilation:
  - Weakly-coupled easy to apply
    - But changing one part can disturb the other
  - Strongly-coupled depends on cross-covariances
    - EnKF uses linear regression – variables not well defined
- Unified software helps to bring new developments into usage
  - PDAF – Open source available at <http://pdaf.awi.de>